

Bernhard Hidding
**Fundamentals and Applications
of Hybrid LWFA-PWFA**

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Strathclyde Centre for Doctoral Training P-PALS
Plasma-based Particle and Light Sources <http://ppals.phys.strath.ac.uk/>

Strathclyde Space Institute
& The Cockcroft Institute

The need for high energy particles has led to greatest machines in the world

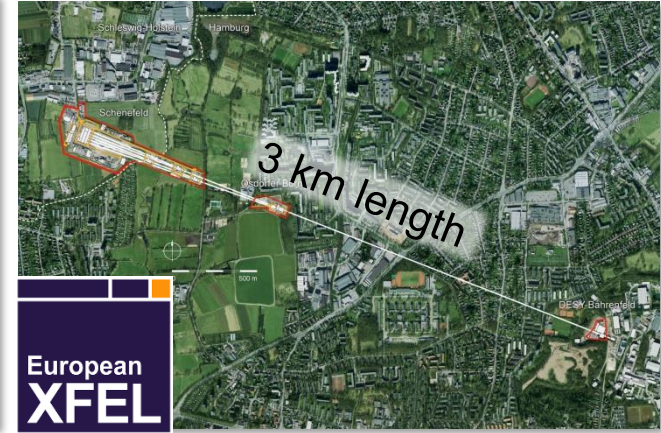
Photons: e.g.



Diamond Light Source,
Synchrotron, Oxfordshire, UK



Linac Coherent Light Source,
X-ray FEL, SLAC, USA



European X-Ray Free Electron
Laser, Hamburg, Germany

Particles: e.g.



Facilities size is the result of limited accelerating electric fields

- Huge particle energies are needed to resolve molecular and atomic structures
- Accelerating electric fields in conventional accelerators are limited to the ~50 MV/m level, because of breakdown of accelerating cavity walls (Kilpatrick criterion*), involving production of “microplasmas”



- Energy gain W is given by the product of charge q , electric field E and acceleration length d : $W = qEd$
- As particle charge is constant and fields are limited, the only way to reach high particle energies is to increase the acceleration distance, i.e. the length of the (linear) accelerator d

* “*Criterion for Vacuum Sparking Designed to Include Both RF and DC*”, W.D. Kilpatrick, *Review of Scientific Instruments* (1957)

THE REVIEW OF SCIENTIFIC INSTRUMENTS

VOLUME 28, NUMBER 10

OCTOBER, 1957

Criterion for Vacuum Sparking Designed to Include Both rf and dc*

W. D. KILPATRICK

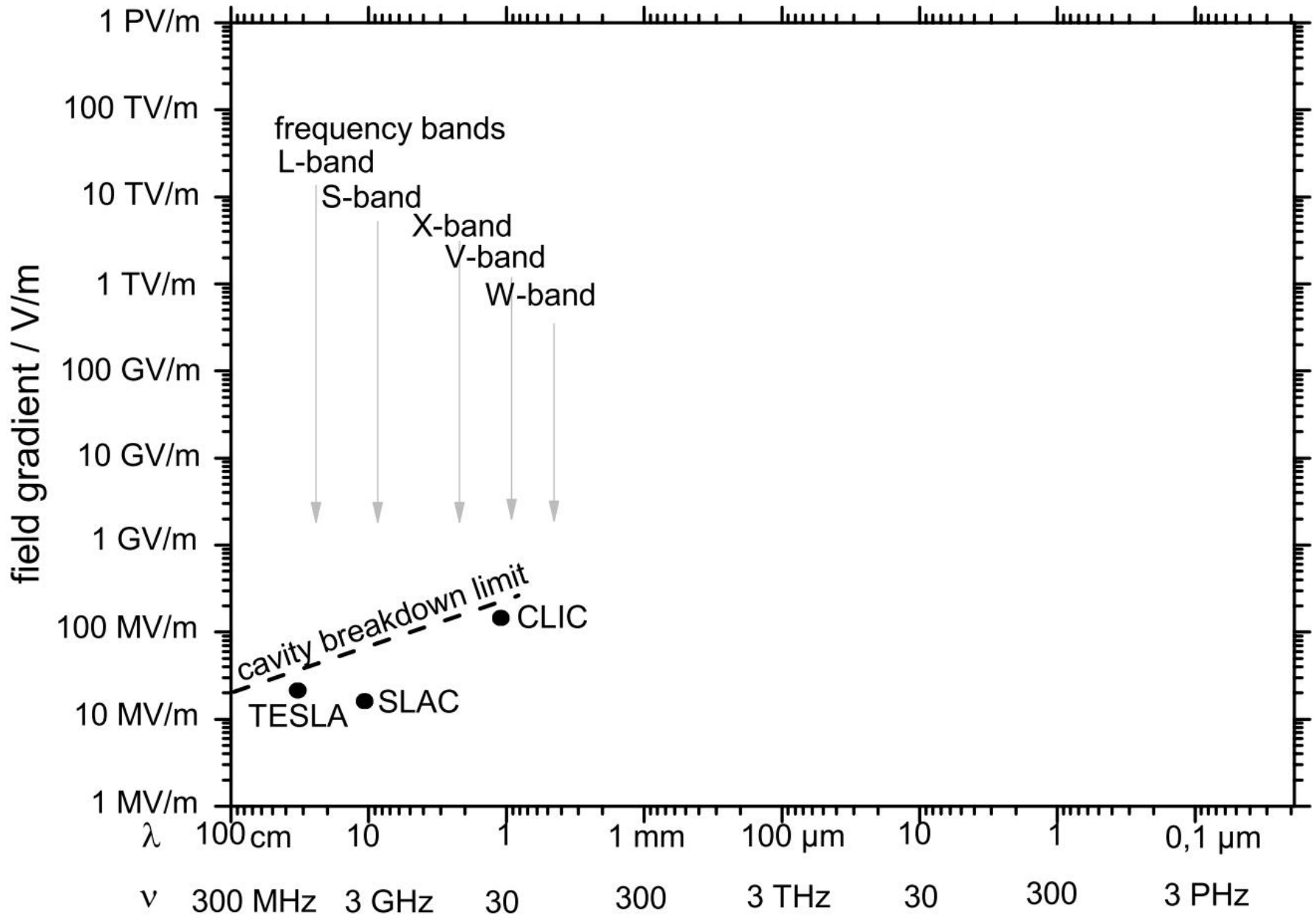
Radiation Laboratory, University of California, Berkeley, California

(Received May 31, 1957)

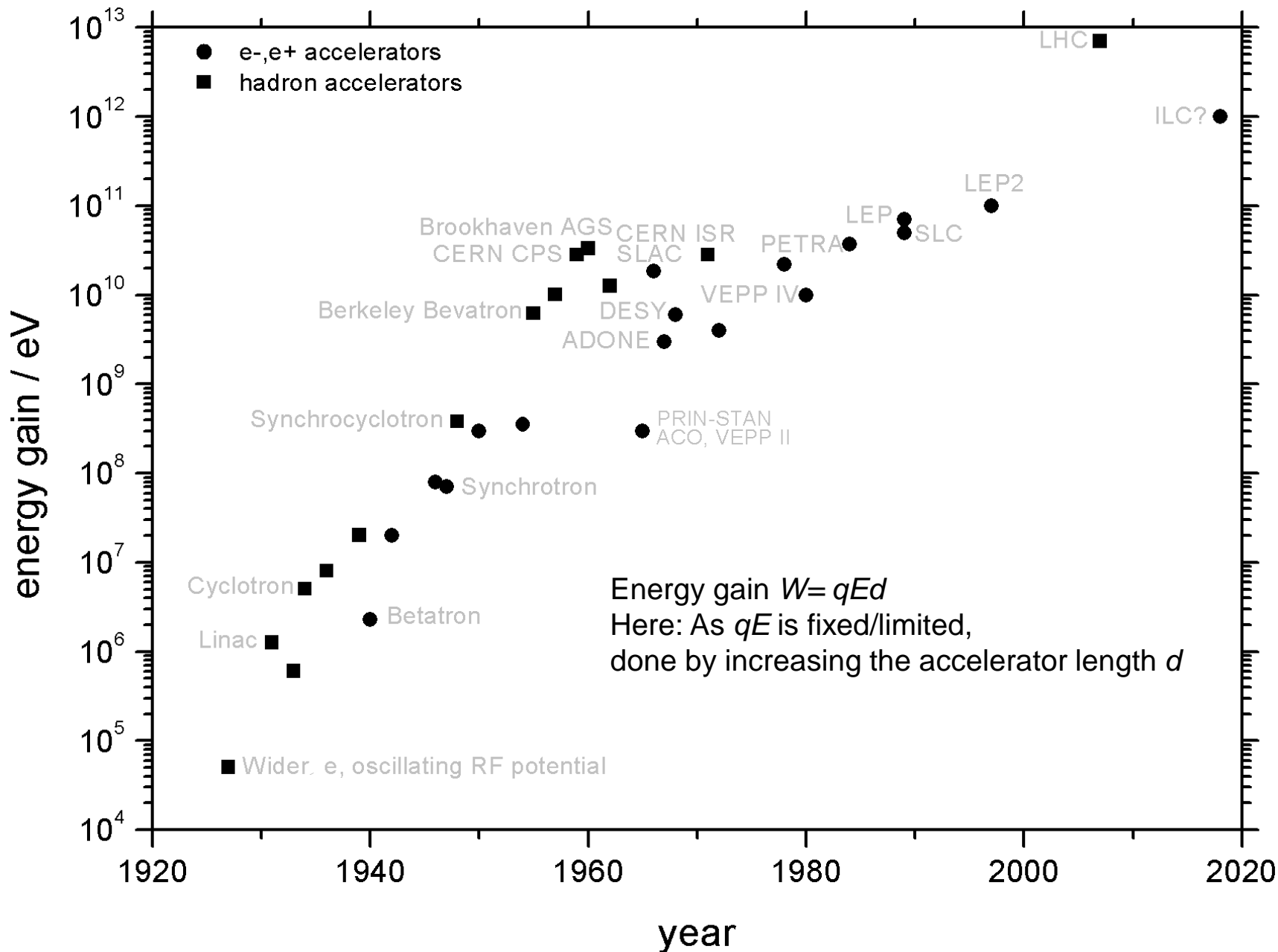
An empirical relation is presented that describes a boundary between no vacuum sparking and possible vacuum sparking. Metal electrodes and rf or dc voltages are used. The criterion applies to a range of surface gradient, voltage, gap, and frequency that extends over several orders of magnitude. Current due to field emission is considered necessary for sparking, but—in addition—energetic ions are required to initiate a cascade process that increases the emitted currents to the point of sparking.

*Increasing the rf frequency increases the obtainable accelerating gradient**

**true in first approximation up to ~X-band, one can go beyond Kilpatrick.. very complex physics..*



Livingston plot: "Moore's Law" for accelerators



First “particle acceleration” experiments:

e.g. Rutherford/Geiger 1911

World’s first particle accelerator experiment: **Matter consists of electrons and ions**



E. Rutherford, Phil. Mag. 21, 1911

The Birth of "Plasma"

LEWI TONKS

407 Oakridge Drive, Schenectady, New York

(Received 24 April 1967)

The origin of the "plasma" of gaseous electronics need not be mythological. The author was there.

THE word *plasma* has achieved universal and unquestioned usage in the description of phenomena in ionized gases and has, at times, even been applied to such other nonphysiological entities as flames, electrolytes, conductors at low temperatures, and the Heaviside layer. Yet how a term, which four decades ago was only used to describe a part of the blood, came to be used in this new sense has never been authoritatively told. There have been a number of guesses, some of them stated as fact, which elaborated on the knowledge that Irving Langmuir initiated the usage. At least one is far more vivid and colorful than the actual event.¹ Had the authors' putative date been correct, I would have been tempted to leave the imaginative extravaganza unquestioned.

As I was working with Langmuir at the time that he appropriated "plasma" for gaseous electronics and I was the only scientist present at the event, I am surely the one most able to give an authoritative account of it. Incidentally, Langmuir's notebooks and mine have both been searched in vain for the first adaptation of "plasma" to the low-pressure arc, the object of our investigations at the time. The first written use (excluding unknown correspondence) must, therefore, have been in the manuscript of "Oscillations in Ionized Gases" [Proceedings of

"Say, Tonks, I'm looking for a word. In these gas discharges we call the region in the immediate neighborhood of the wall or an electrode a 'sheath,' and that seems to be quite appropriate; but what should we call the main part of the discharge? The conductivity is high so that you can't apply a potential difference to it like you can to a sheath—it all is taken up by the sheaths. And there is complete space-charge neutralization. I don't want to invent a word, but it must be descriptive of this kind of region as distinct from a sheath. What do you suggest?"

My reply was classic: "I'll think about it, Dr. Langmuir."

The next day Langmuir breezed in and announced, "I know what we'll [*sic*] call it! We'll call it the 'plasma.'" The image of blood plasma immediately came to mind; I think Langmuir even mentioned blood. In the light of the contemporary state of our knowledge, the choice seemed very apt.

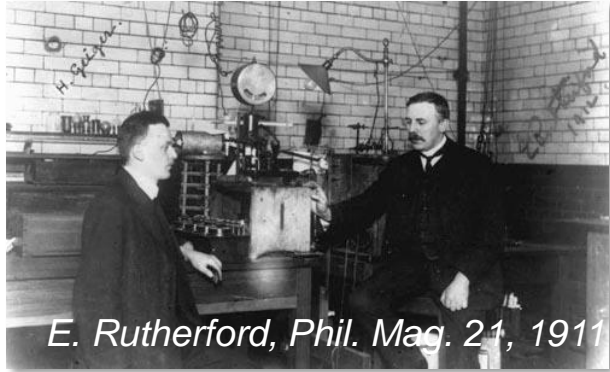
Our attention was focused on the laboratory experiments. The extensive broadening of concept which would include electrolytes, flames, the Heaviside layer, etc. may have lain in the back of Langmuir's brain. The semantic problem to be solved was sheath vs nonsheath.

Quite definitely, neither the oscillatory characteristics of plasmas nor "the seething move-

Prehistoric days: Plasma Wakefield Acceleration

Rutherford/Geiger 1911

World's first particle accelerator experiment:
Matter consists of electrons and ions



Langmuir/Tonks 1928

“We shall use the name *plasma* to describe [a] region containing balanced charges of ions and electrons”

CERN 1956

Future particle accelerators:
Accelerate particles via collective fields by separating electrons and ions in plasmas
Veksler, Budker, Fainberg, Proc. CERN Symp. High Energy Accelerators, 1956

Project Matterhorn

Description and computation of nonlinear plasma oscillations

J. Dawson, Phys. Rev. 113, 383, 1959

UCLA 1979: **LWFA**

Produce transient charge separation in plasma via Laser Electron Accelerator

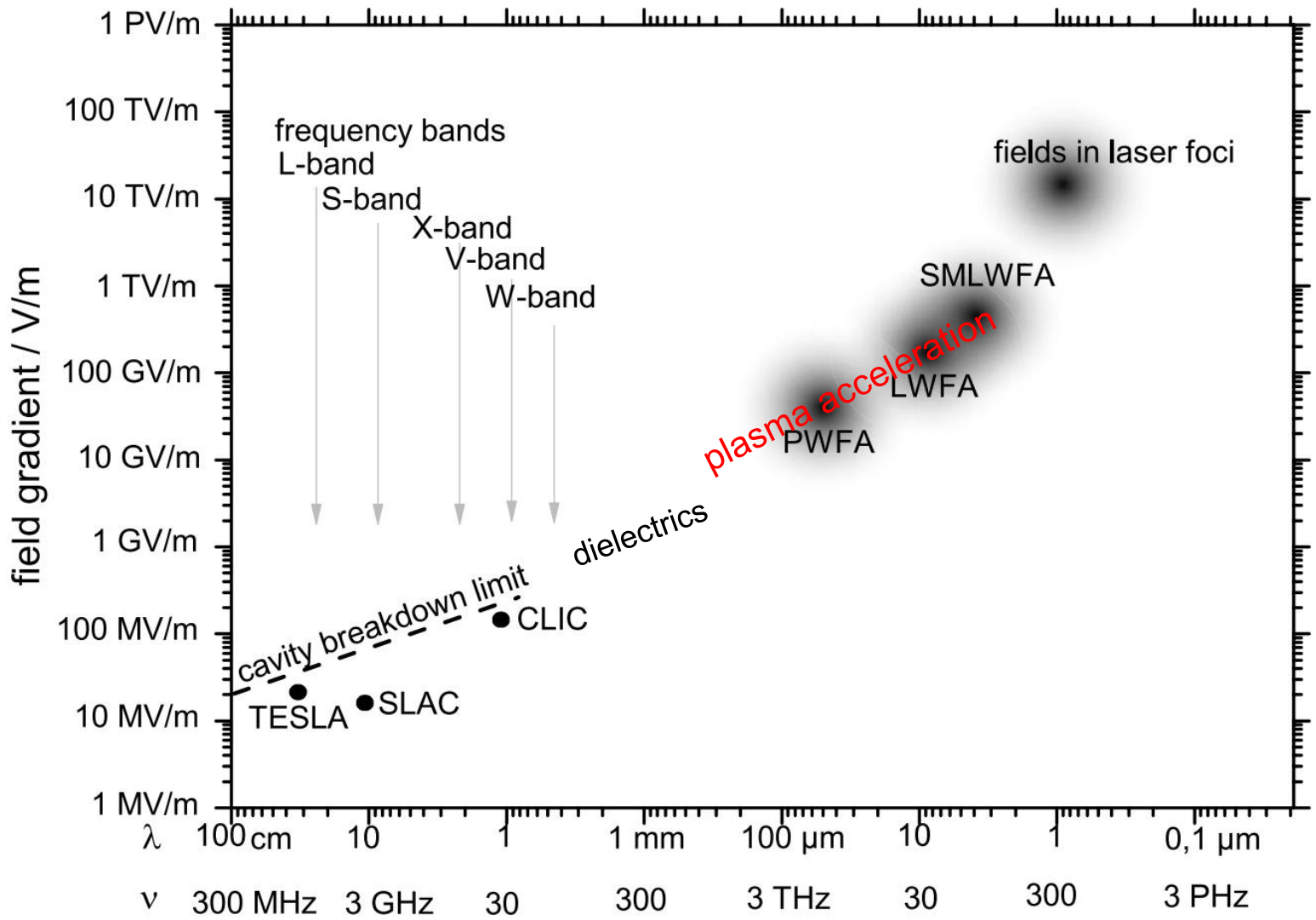
Tajima & Dawson, Phys. Rev. Letters 43, 1979

Stanford/UCLA 1985: **PWFA**

Acceleration of Electrons by the Interaction of a Bunched Electron Beam with a Plasma

Chen et al., Phys. Rev. Letters 54, 1985

Plasma: tens of GV/m+ acceleration gradients allow shrinking of accelerator to sub-meter scale (energy gain $W=qED$)



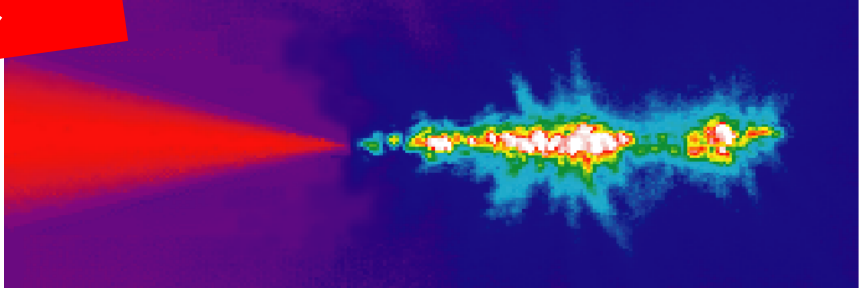
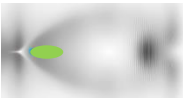
Shrinking accelerators from km to cm size



Multiple static metallic cavities
w/ electric fields of ~ 50 MV/m



Single co-propagating plasma cavity
w/ electric fields of ~ 50 GV/m

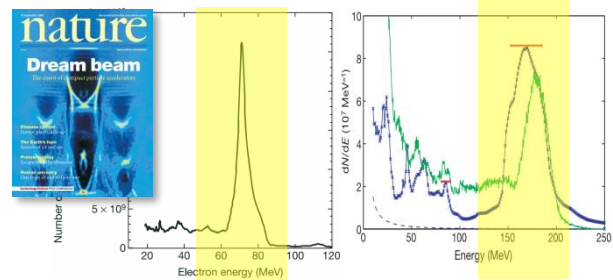


0 100 200 300

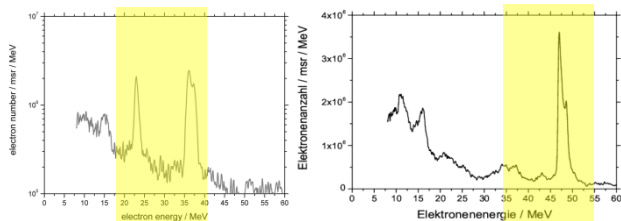
channel length / μm

Indeed: Both LWFA (laser driven) and PWFA (electron beam driven) now routinely demonstrate multi-GeV energy gain

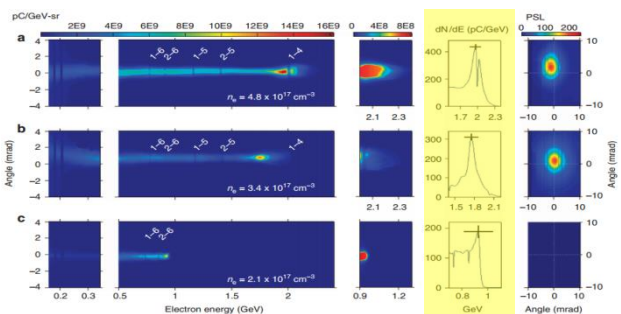
LWFA



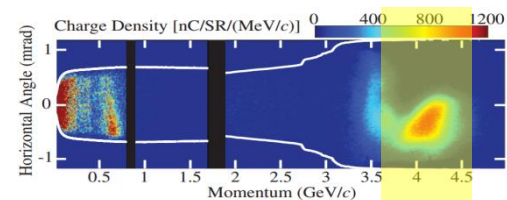
Mangles et al. (UK), Geddes et al. (USA), Faure et al. (France), Nature 2004



Hidding et al., PRL 2006

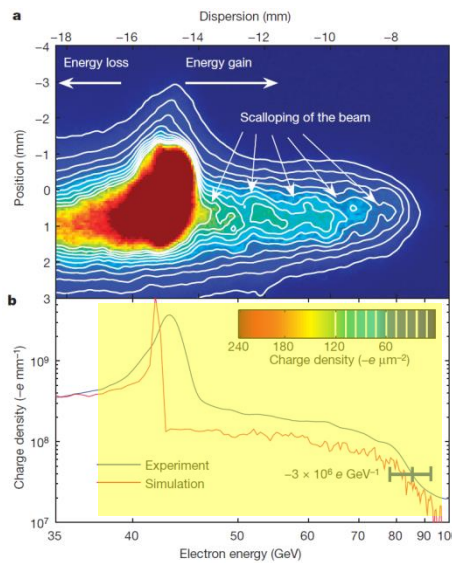


Wang et al., Nat. Comm. 2013

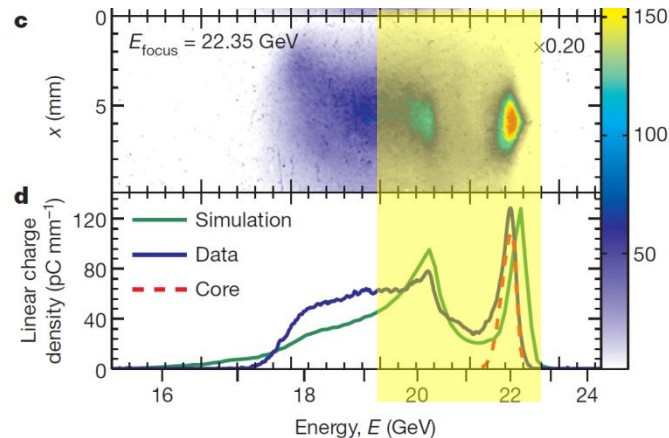
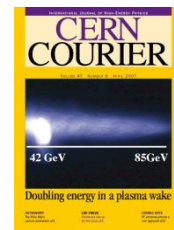


Leemans et al., PRL 2014

PWFA

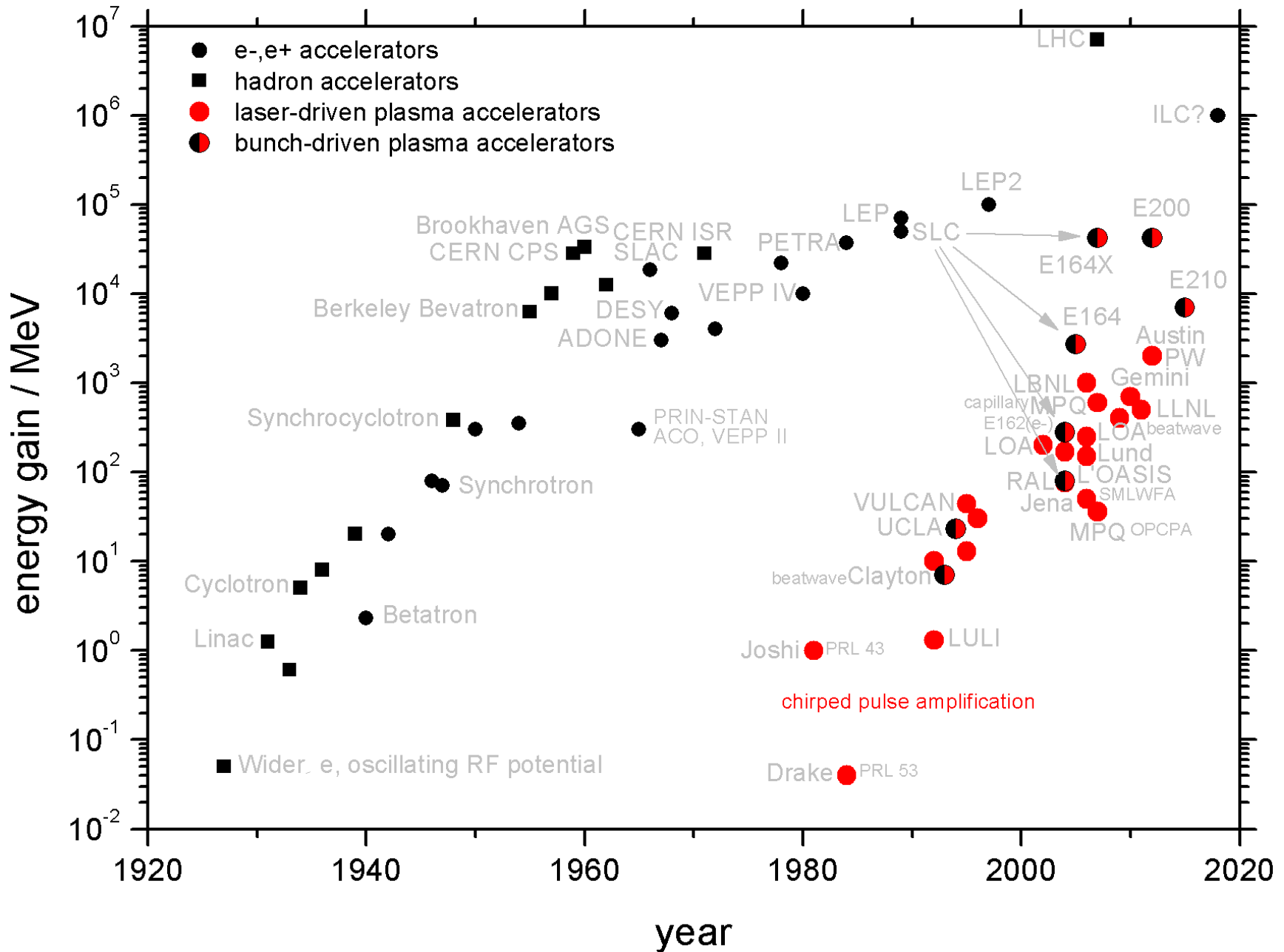


Blumenfeld et al., Nature 2007



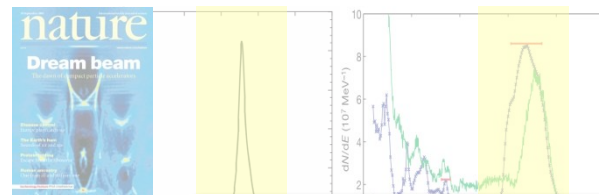
Litov et al., Nature 2014

Livingston plot: *with plasma accelerators* (ignoring beam quality etc.)

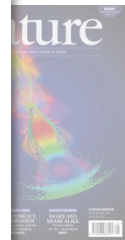
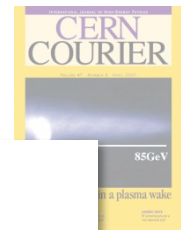
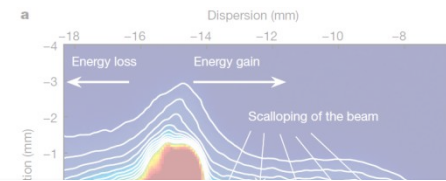


Indeed: Both LWFA and PWFA routinely demonstrate multi-GeV energy gain

LWFA



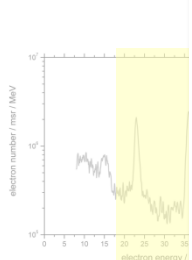
PWFA



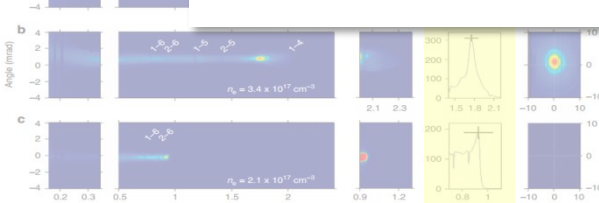
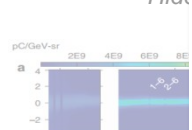
- *Fantastic energy gains, increase of energy & beam quality by order of magnitude in a decade, ultrashort & high current (many kA), ongoing steady progress..*
- *But: stability, tunability, beam quality so far still limited*
- *Another game-changer is required..*



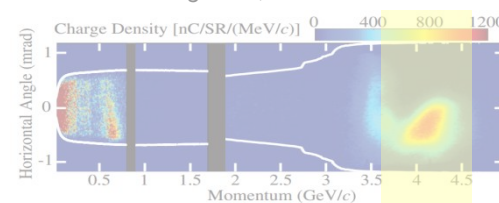
Mangles et Faure et



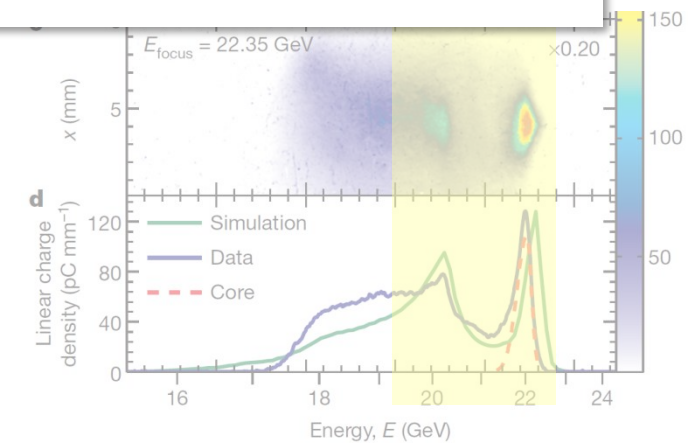
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Wang et al., Nat. Comm. 2013



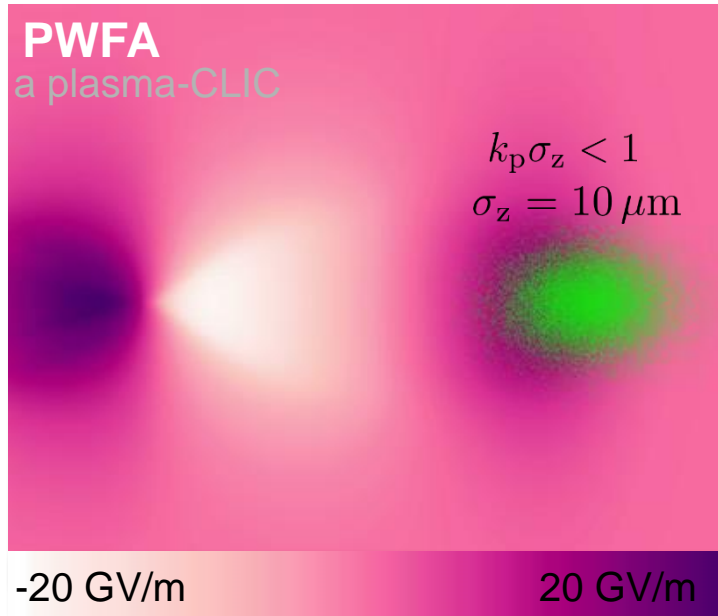
Leemans et al., PRL 2014



Litos et al., Nature 2014

Hybrid LWFA & PWFA

Many similarities between PWFA “blowout” and LWFA “bubble” generation...



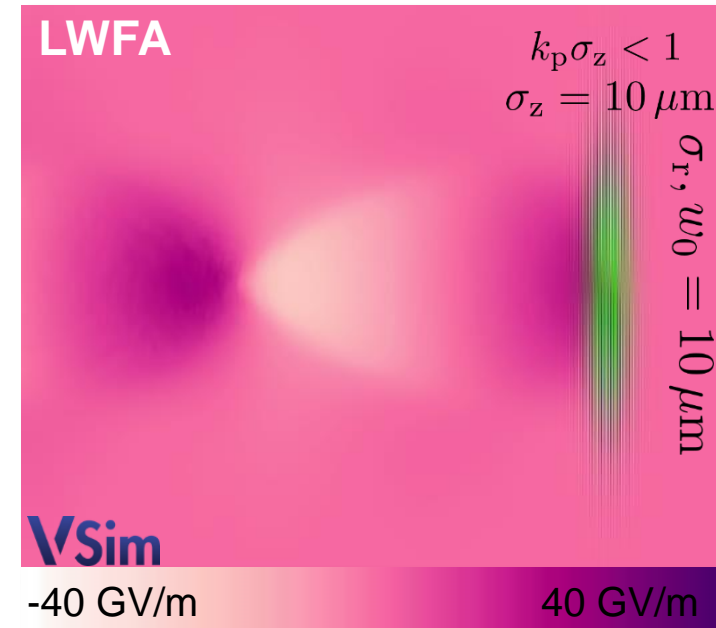
plasma density
 $n_p = 10^{17} \text{ cm}^{-3}$

plasma wavelength
(i.e. blowout/bubble size)
 $\lambda_p \approx 106 \mu\text{m}$

plasma skin depth
 $k_p^{-1} \approx 16 \mu\text{m}$

dimensionless beam charge
 $\tilde{Q} = \frac{N_b k_p^3}{n_p} \approx 3$

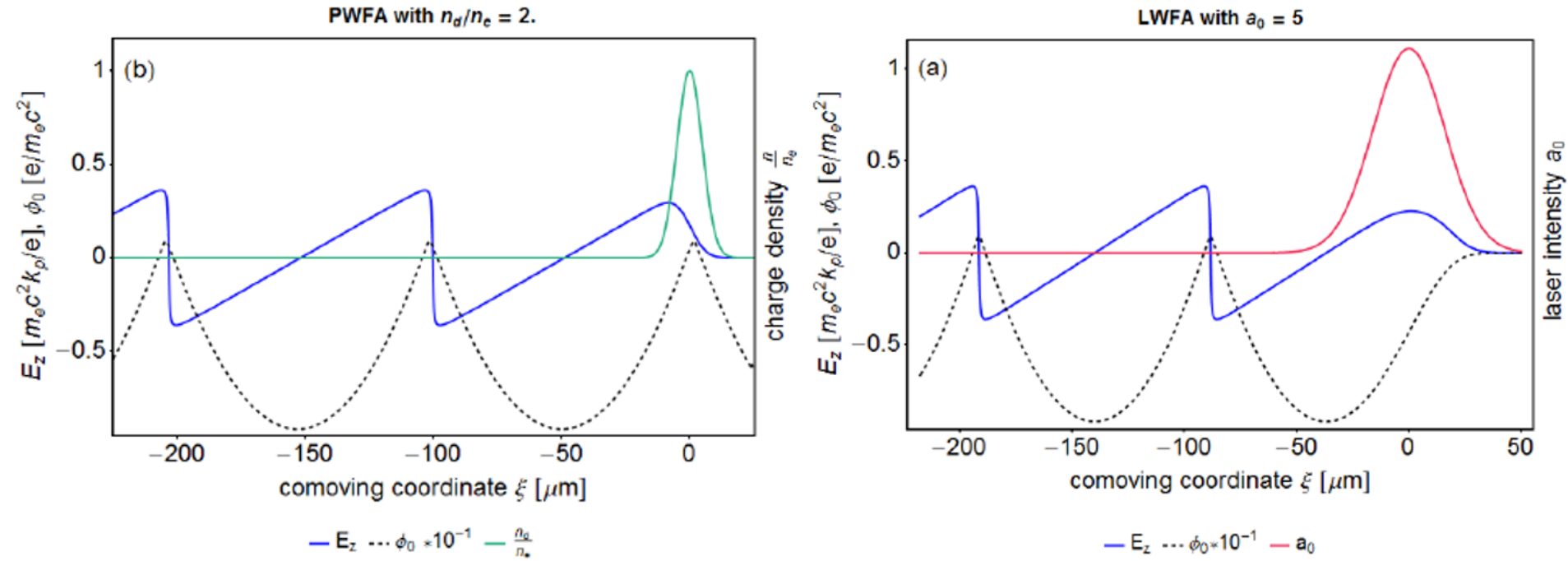
$$\tilde{Q} = \frac{N_b k_p^3}{n_p} \begin{cases} < 0 & \text{linear regime} \\ \approx 0 & \text{quasilinear} \\ > 0 & \text{nonlinear (blowout regime)} \end{cases}$$



dimensionless light amplitude
 $a_0 = \frac{eE}{m_0 \omega c} \approx 3$

- PWFA: Chen et al. PRL 1985, Rosenzweig et al. PRL 1988, Rosenzweig et al. PRA 1990, Assmann et al. SLAC 1998, Blumenfeld et al. 2007, Litos et al. Nature 2014
- LWFA: Tajima & Dawson PRL 1979, Clayton et al. PRL 1990, Pukhov & MtV ABP 2002, Faure/Mangles/Geddes et al. Nature 2004, Leemans et al. PRL 2014

Plasma wake excitation



- 1D nonlinear model in co-moving frame (quasi-static approximation):

$$\frac{\partial^2 \phi}{\partial z^2} = -\frac{4\pi e}{m_e c_0^2} \rho$$

Poisson

$$\begin{aligned} \frac{\partial^2 \phi}{\partial z^2} &= \frac{4\pi e^2}{m_e c_0^2} (n_e - n_0 + n_d) \\ &= \frac{4\pi e^2 n_0}{m_e c_0^2} \left(\frac{n_e}{n_0} + \frac{n_d}{n_0} - 1 \right) \\ &= k_p^2 \left(\frac{n_e}{n_0} + \frac{n_d}{n_0} - 1 \right). \end{aligned}$$

$$k_p^{-2} \frac{\partial^2 \phi}{\partial \xi^2} = \underbrace{\frac{n_d}{n_0}}_{\text{e-beam}} + \underbrace{\frac{1 + a_0^2}{2(1 + \phi)^2}}_{\text{laser}} - \frac{1}{2}$$

- longitudinal electric field E_z and electrostatic potential ϕ are similar for PWFA and LWFA
- Detailed lecture on this e.g. in Nadjmudin's talk. Script see on SCDT webpage:



Parameters

pulse energy [J]

pulse length (FWHM) [fs]

w0 [μm]

laser wavelength [nm]

plasma density [cm^{-3}]

set EuPraxia defaults

set Ti:Sa 800 nm

set CO2 10600 nm

e-bunch parameters

charge [pC]

σ_z [μm]

σ_r [μm]

$\Delta\xi$ [μm]

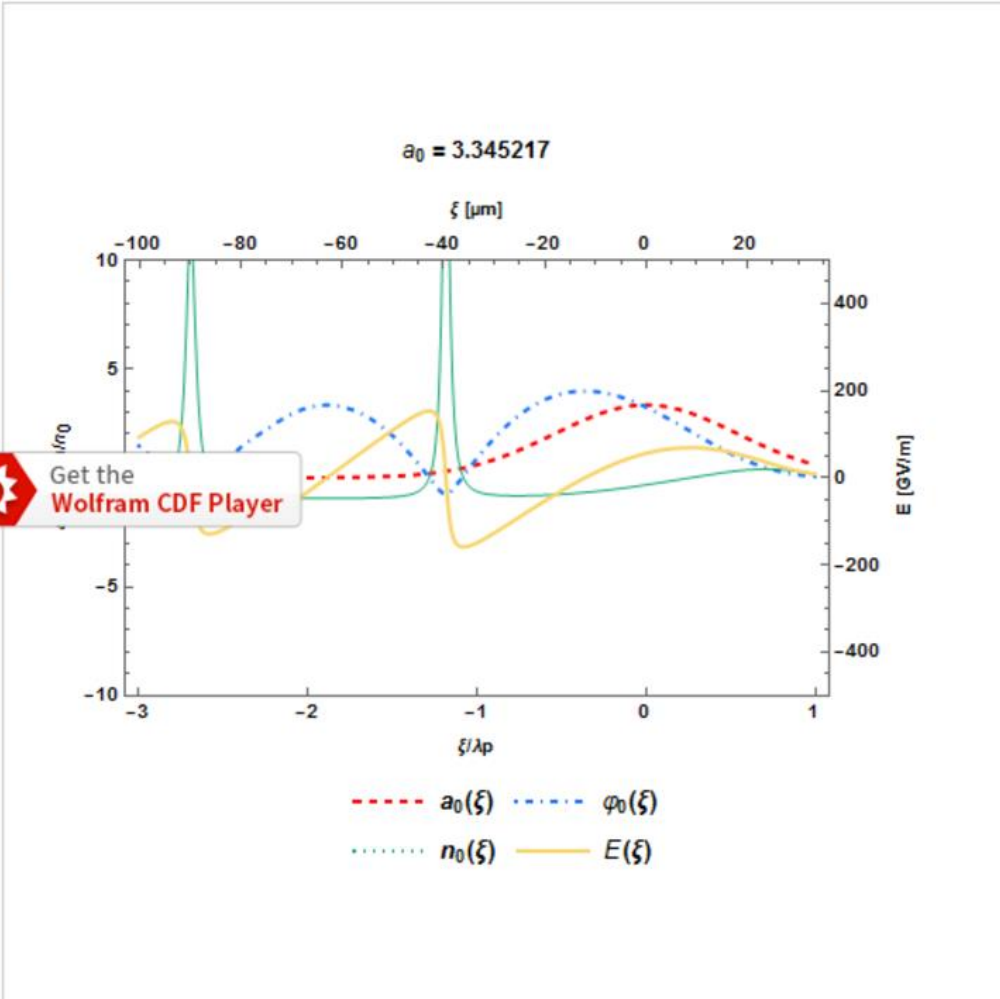
Plot Scaling

plasma periods

left axis scale

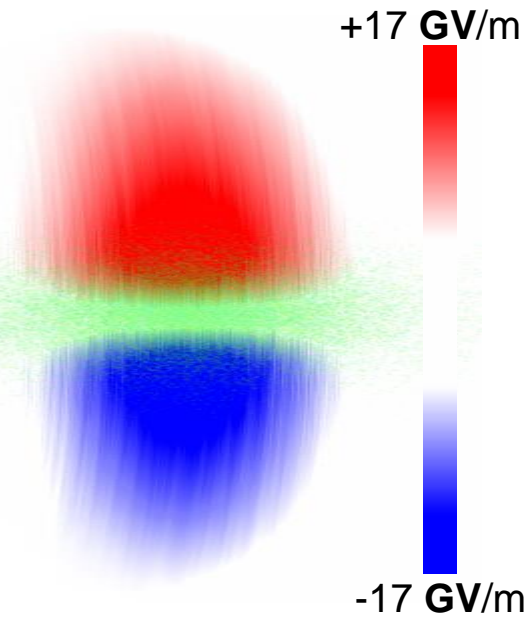
right axis scale

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... but also profound differences: *unipolar (PWFA) vs. oscillating (LWFA) fields*

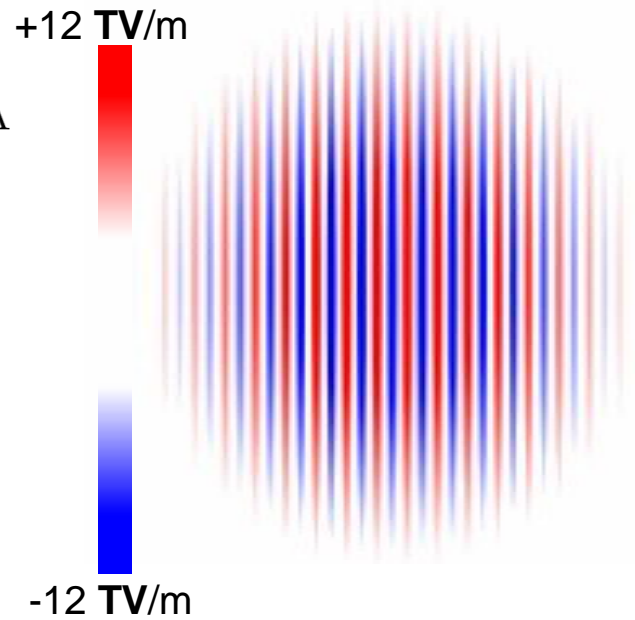
PWFA



$E_{r,PWFA} \ll E_{r,LWFA}$
 while accelerating
 plasma fields are similar

Intuitively clear: you want
 unidirectional fields to
 expel electrons off axis

LWFA



ponderomotive force

$$F_{\text{pond}} = -\frac{e^2}{4m\omega^2} \nabla E^2 \propto \nabla I$$

Coulomb force

$$F_{\text{Coulomb}} = e\mathbf{E}$$

$$E_r(r, z) = \frac{Ne}{2\pi^{3/2}\epsilon_0\sigma_z r} \left[1 - \exp\left(-\frac{r^2}{2\sigma_r^2}\right) \right]$$

⇒ PWFA more efficient to excite plasma wave, LWFA much better to generate plasma

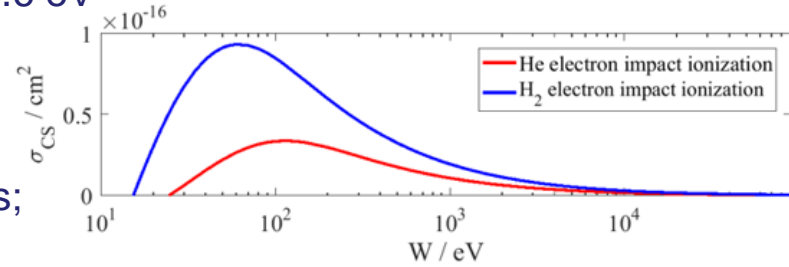
Ionization processes: SPI/MPI, impact ionization, Tunneling, BSI

- No single photon ionization (SPI) at typical laser frequencies: $h\nu \ll \xi_i$ (ionization potential)
For example H2: $\xi_i \approx 15.4$ eV, H: $\xi_i \approx 13.6$ eV, He: $\xi_i \approx 24.6$ eV

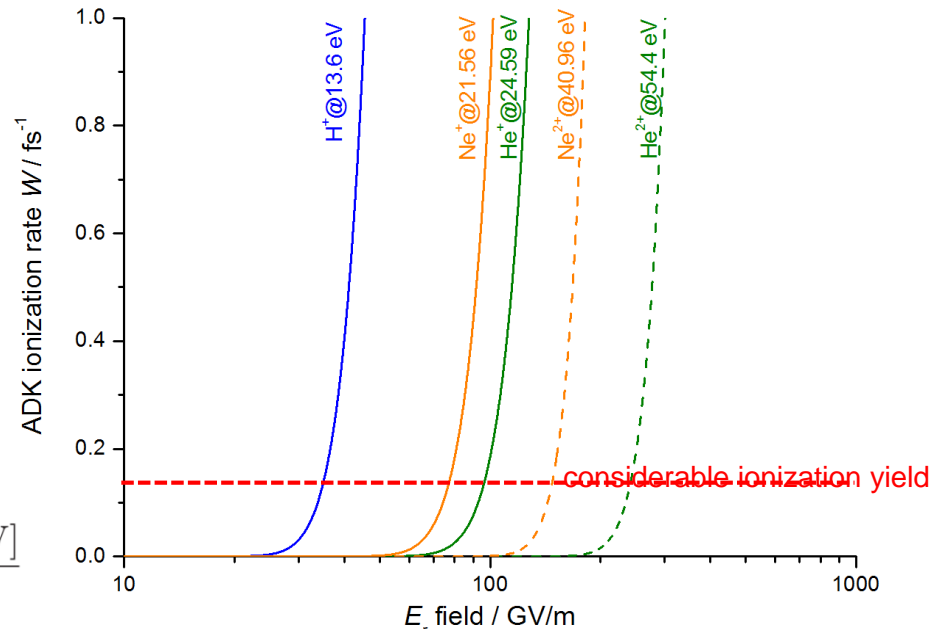
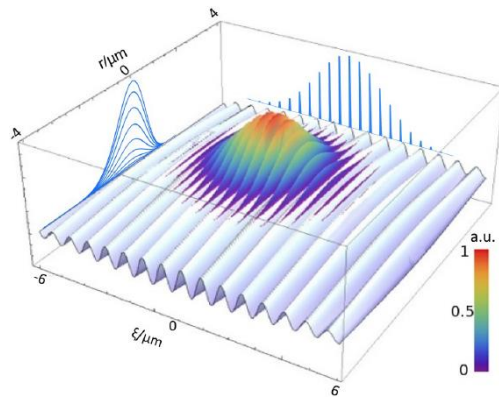
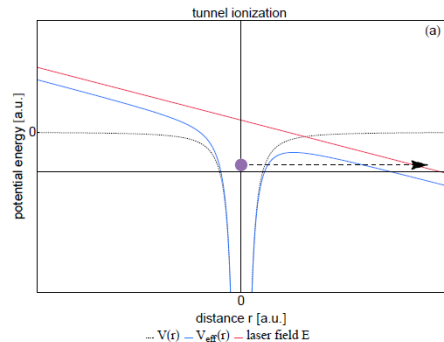
- Impact ionization by electron drive beam negligible:

- Keldysh parameter: $\gamma_k \ll 1$ tunneling ionization dominates; $\gamma_k \gg 1$ MPI dominates. For 800 nm laser wavelength and intensities sufficient to ionize He, MPI negligible.

At higher harmonics (400 nm, 233 nm etc.), MPI is important and Yudin-Ivanov model should be used



- ADK tunneling ionization rates:
$$W(\text{s}^{-1}) \approx 1.52 \times 10^{15} \frac{4^{n^*} \xi_i^{n^*} [\text{eV}]}{n^* \Gamma(2n^*)} \left(20.5 \frac{\xi_i^{3/2} [\text{eV}]}{E [\text{GV/m}]} \right)^{2n^* - 1} \times \exp \left(-6.83 \frac{\xi_i^{3/2} [\text{eV}]}{E [\text{GV/m}]} \right)$$



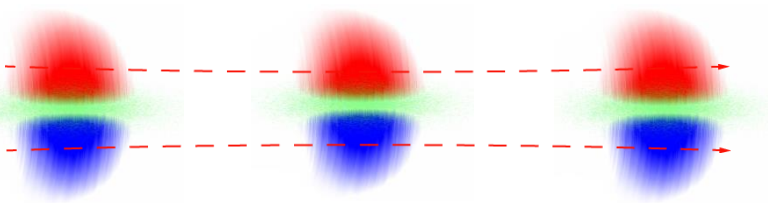
- At even higher intensities, Barrier Suppression Ionization

$$I_{\text{BSI}} [\text{W}/\text{cm}^2] \approx 4 \times 10^9 \frac{\xi_i^4 [\text{eV}]}{Z^2}$$

... also profound differences: *beam expansion (PWFA) vs. diffraction (LWFA)*

PWFA

Electron/photon density needs to stay intense over long acceleration distance



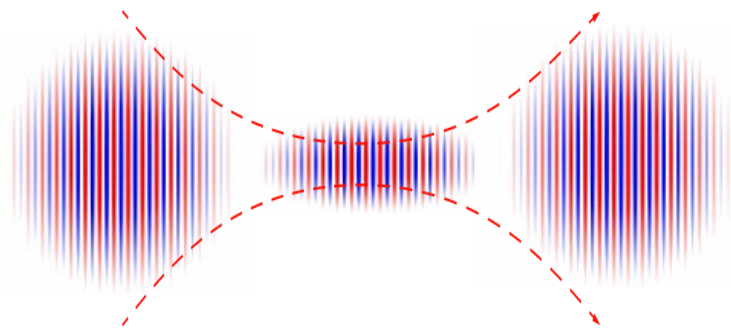
$$\sigma_r(z) = \sigma_{r0} \sqrt{1 + \left(\frac{z}{\beta^*}\right)^2}$$

Both laser and electron beam expands hyperbolically, but

Betatron length $\beta^* = \sigma_{r0}^2 \gamma / \epsilon_n$

e.g., $\beta^* \approx 20 \text{ cm}$ at $\sigma_{r0} = 10 \mu\text{m}$,
 $\gamma = 2000$, $\epsilon_n = 10^{-6} \text{ mrad}$

LWFA



$$\omega(z) = \omega_0 \sqrt{1 + \left(\frac{z}{Z_R}\right)^2}$$

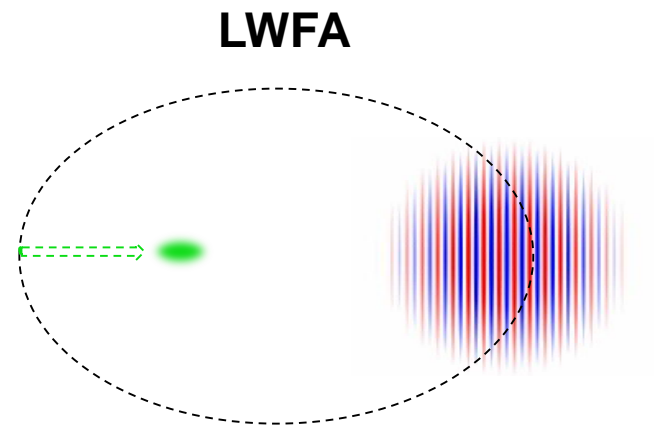
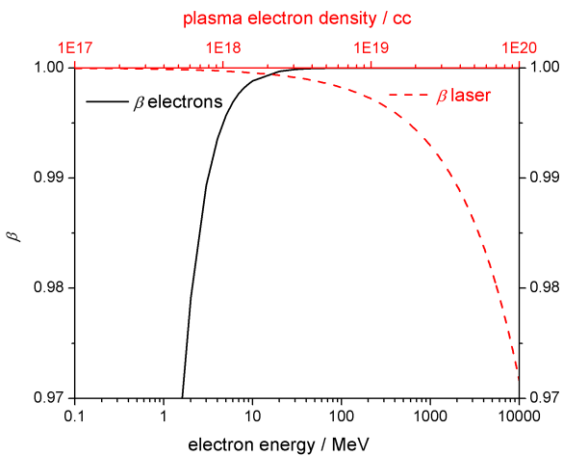
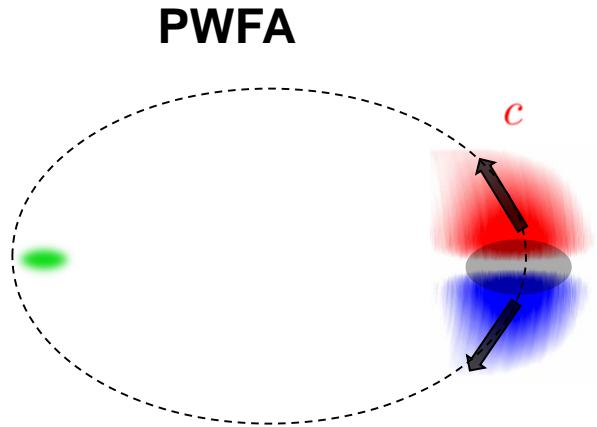
Rayleigh length $Z_R = \pi \omega_0^2 / \lambda$

e.g., $Z_R \approx 400 \mu\text{m}$ at $\omega_0 = 10 \mu\text{m}$
 Ti:Sa laser (0.8 μm)

*⇒ PWFA allows orders of magnitude longer acc. distances w/o any tricks (guiding etc.),
 LWFA allows to interact in very confined volume*

... also profound differences: *dephasing*

Electrons to be accelerated need to stay in proper phase of plasma wave



Electron beam(s) moves with c

⇒ witness bunch stays in proper phase and harnesses max. acc. fields

⇒ No dark current: self injection difficult because wake moves fast:

$\gamma_{wake} = \gamma_{driver} = 10^4$ e.g. for 10 GeV drive beam

Laser beam moves with group velocity in plasma

$$v_g = c \left(1 - \frac{\omega_p^2}{\omega_0^2} \right)^{1/2} < c$$

⇒ witness bunch moves forward, samples different field regions and reaches dephasing limit after distance

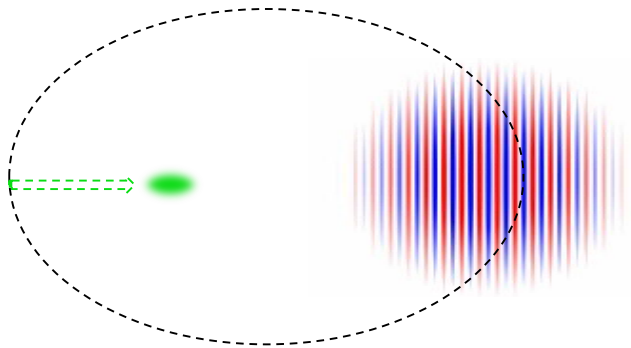
$$L_d \approx \lambda_p^3 / \lambda^2 = n_c / n_e^{3/2}$$

⇒ Self injection / dark current easy because $\gamma_{wake} = \gamma_{laser} \approx 10-100$ for typical densities

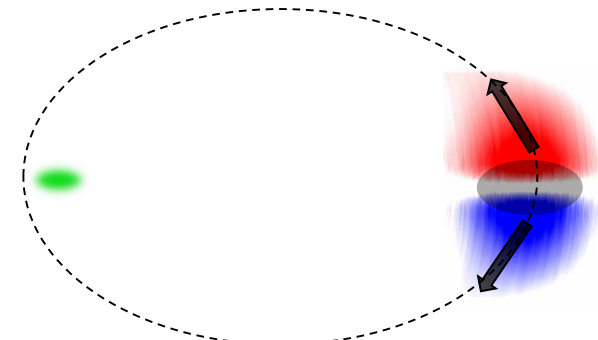
⇒ *PWFA allows orders of magnitude longer acc. distances w/o dephasing, while dephasing can help make bunches “monoenergetic” w/ LWFA*
 ⇒ *LWFA allows for easier self-injection, while PWFA in turn easily dark current free*

LWFA vs PWFA summarized

- Electron bunches: drive plasma wave efficiently due to unidirectional fields
- Lasers w/ oscillating field structure only able to drive plasmas due to ponderomotive force
- Lasers can easily ionize matter, because of diffraction can do so in very confined area
- Electron bunches can be produced with very high rep rate from state-of-the-art sources
- Electron bunches are not good for ionizing matter
- Electron bunches move with c , allow for dephasing-free accelerator systems
- No dark current in PWFA systems because of high gamma
- Electron bunches are stiff: don't expand much transversally (limited diffraction) – long acc. distances



ionization @ $\sim 10^{14}$ W/cm² (easy)
bubble @ $\sim 10^{18}$ W/cm² (hard)



ionization if $E_r > 5$ GV/m (hard)
blowout if $n_b > n_e$ (easy)

⇒ Electron bunches are better plasma drivers, laser pulses great for injection!

Injection and trapping

- Trapping: accelerating electrons must catch up with wave so that $\gamma_{\text{electron}} \geq \gamma_{\text{wave}} = \gamma_p$
- If electrons initially at rest, trapping condition: wake electrostatic potential energy \geq kinetic energy the electrons need to gain

$$-e\Delta\phi' \geq E'_{\text{kin}} = E_0(\gamma_p - 1) = m_0c^2(\gamma_p - 1)$$

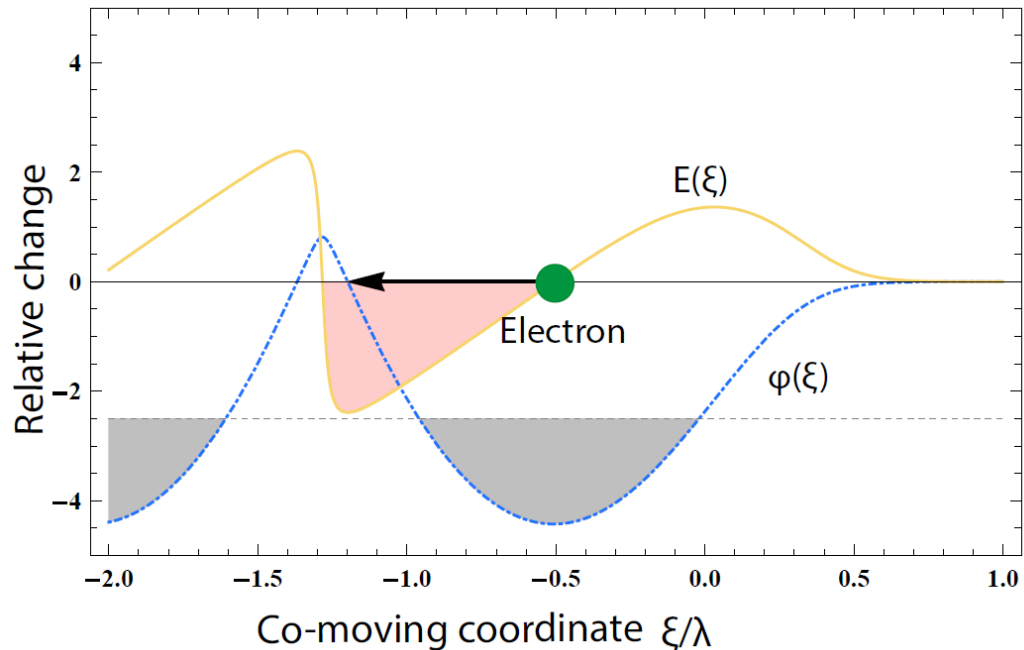
Hamiltonian of electron in electromagnetic field:

$$\mathcal{H} = \underbrace{\gamma mc^2}_{\text{electron energy}} - \underbrace{e\phi}_{\text{scalar potential}}$$

Where is trapping the easiest?

Right in center of the blowout: an electron released there always sees accelerating fields, and can catch up with the plasma wave most easily.

Great spot to release electrons for injection – but how to put them there?



Relativistic identities

$$\vec{\beta} = \frac{\vec{v}}{c} = \sqrt{1 - \frac{E_0^2}{(E + E_0)^2}} \cdot \frac{\vec{v}}{|\vec{v}|} = \sqrt{1 - \frac{1}{\gamma^2}} \cdot \frac{\vec{v}}{|\vec{v}|} = \frac{\vec{p}}{\sqrt{(m_0 c)^2 + p^2}}$$

Lorentz factor:

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}} = \sqrt{1 + \frac{p^2}{(m_0 c)^2}} = \frac{\sqrt{(m_0 c)^2 + p^2}}{m_0 c} = \frac{E}{E_0} + 1$$

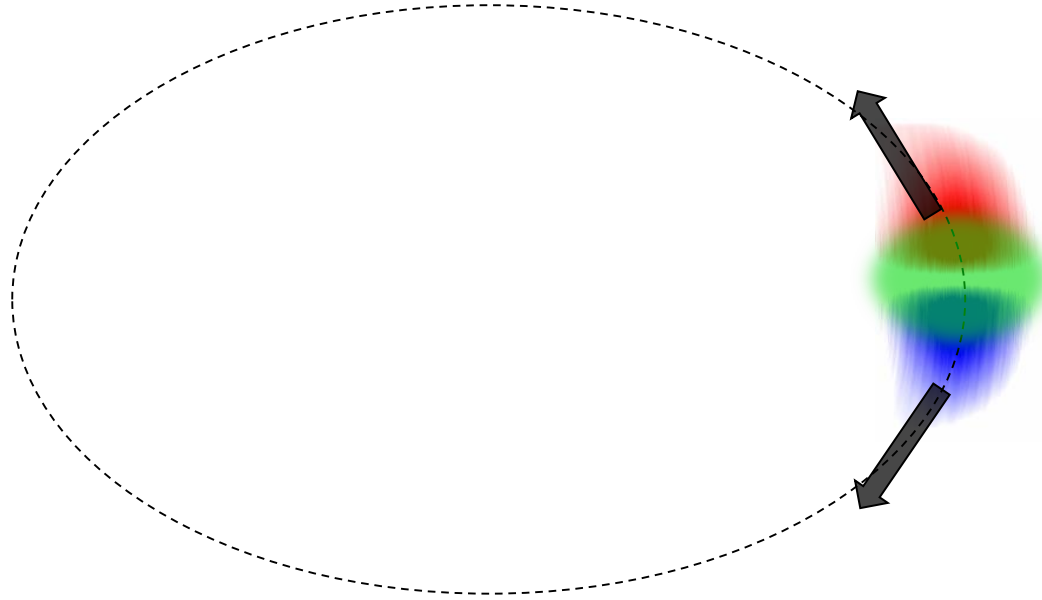
In contrast: phase velocity of plasma wave γ_p driven by laser pulse is the group velocity of laser pulse, which is plasma electron density-dependent

$$v_g = c \left(1 - \frac{\omega_p^2}{\omega_0^2} \right)^{1/2} < c$$

$$\vec{p} = m_0 c \gamma \vec{\beta} = m_0 c \sqrt{\gamma^2 - 1} \cdot \frac{\vec{v}}{|\vec{v}|} = m_0 c \sqrt{\frac{\beta^2}{1 - \beta^2}} \cdot \frac{\vec{v}}{|\vec{v}|} = \sqrt{\frac{E^2}{c^2} + 2E m_0} \cdot \frac{\vec{v}}{|\vec{v}|}$$

$$E_{kin} = E_0 (\gamma - 1) = E_0 \left(\sqrt{1 + \frac{p^2}{(m_0 c)^2}} - 1 \right) = E_0 \left(\frac{1}{\sqrt{1 - \beta^2}} - 1 \right)$$

Trojan Horse: Underdense Plasma Photocathode & Wakefield Acceleration

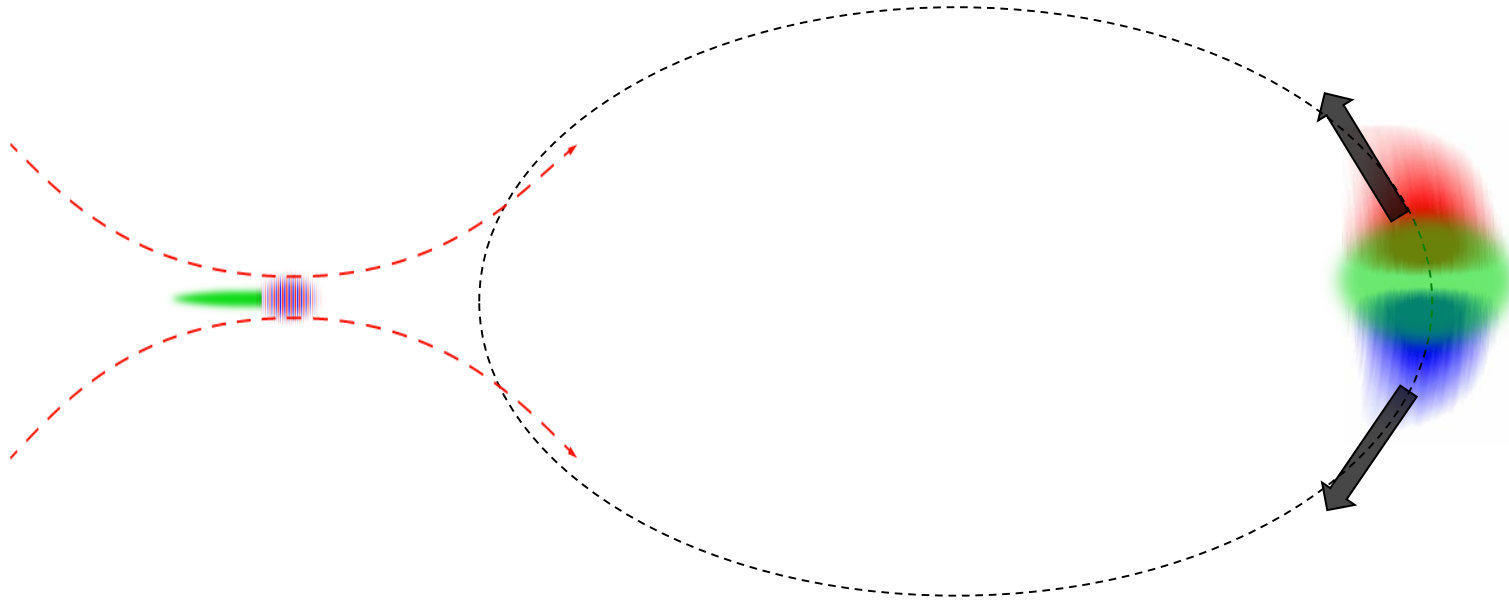


Step 1

- Electron beam driver sets up dephasing free, dark current free plasma cavity in low-ionization threshold (LIT) plasma such as hydrogen ($\xi_i \approx 13.6$ eV)
- A high-ionization threshold (HIT) gas is present such as Helium ($\xi_i \approx 24.6$ eV), not ionized by driver nor wake (density can be tuned independently of LIT density)

$$I_{\text{BSI}} [\text{W}/\text{cm}^2] \approx 4 \times 10^9 \frac{\xi_i^4 [\text{eV}]}{Z^2}$$

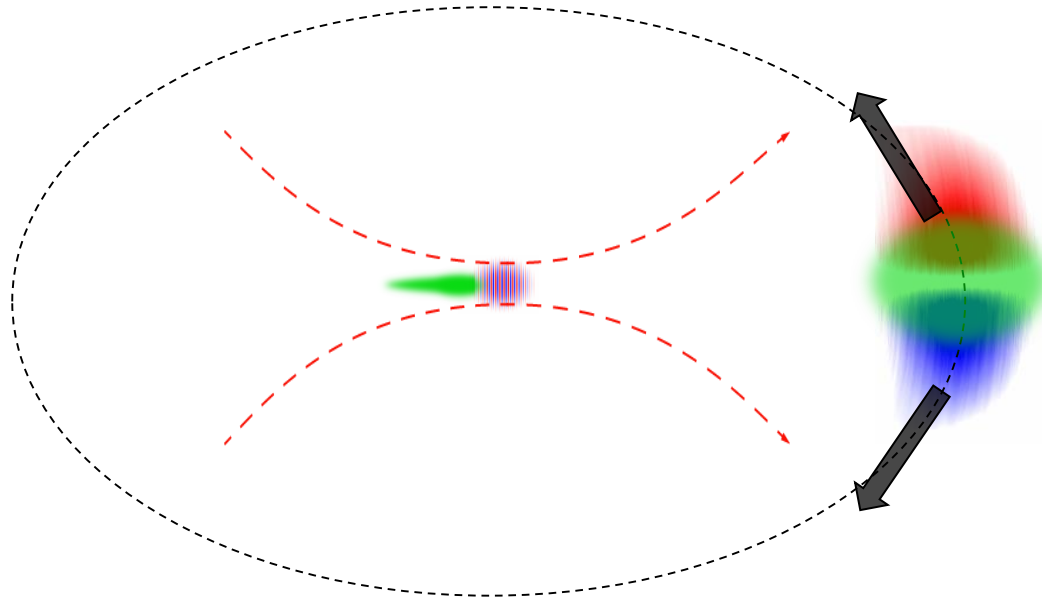
Take the best of both worlds: Hybrid Plasma Acceleration



Step 2

- A synchronized, low intensity laser pulse is focused strongly to the HIT level, releases He electrons in confined volume at arbitrary position
- Tune released He electrons (i.e. charge) with He density, a_0 , w_0 , ω , τ , polarization, focus shape...

Take the best of both worlds: Hybrid Plasma Acceleration

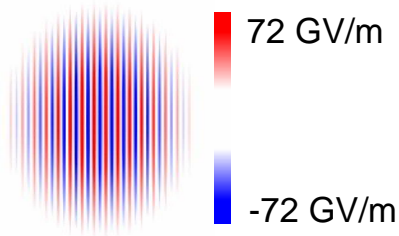


Step 3

- Released He electrons fall behind but are compressed and trapped in ideal phase
- Ultracold electrons are rapidly accelerated (mitigating space charge effects) and are accelerated as long as driver can excite plasma wave

Why witness bunches ultracold?

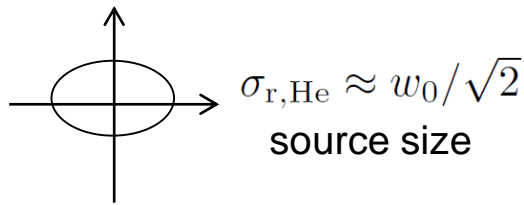
Laser kick contrib. to norm. emittance:



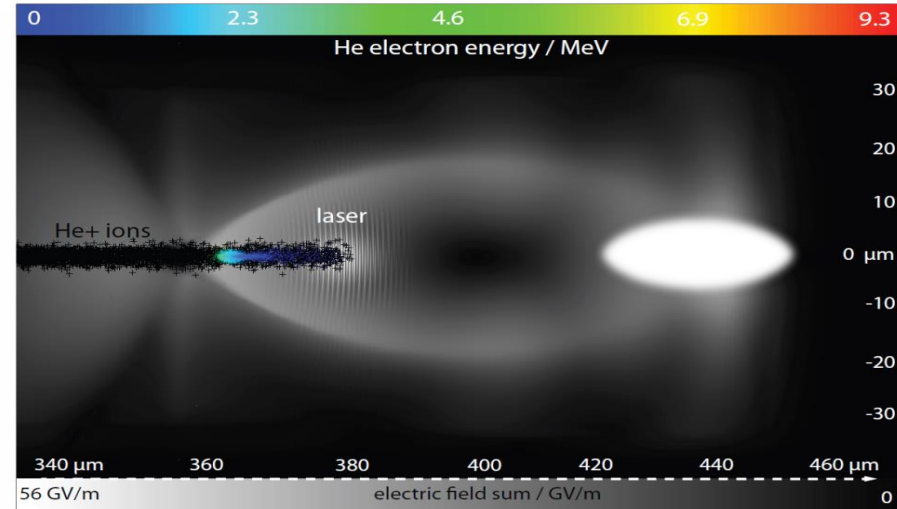
$$E_0 = a_0 \frac{2\pi m_e c^2}{e\lambda}$$

$$\sigma_{p_r} / (mc) \approx a_0 / 2$$

residual momentum



$$\epsilon_n \approx \sigma_{r,HIT} \sigma_{p_r,HIT} / (mc) \approx \boxed{w_0 a_0} / 2^{3/2} \text{ crude scaling}$$



$$\epsilon_y \approx \epsilon_x = k_p w_i^2 a_i \left(\frac{3\pi r_e}{4\sqrt{2}\alpha^4 \lambda_i} \right) \left(\frac{U_H}{U_I} \right)^{3/2}$$

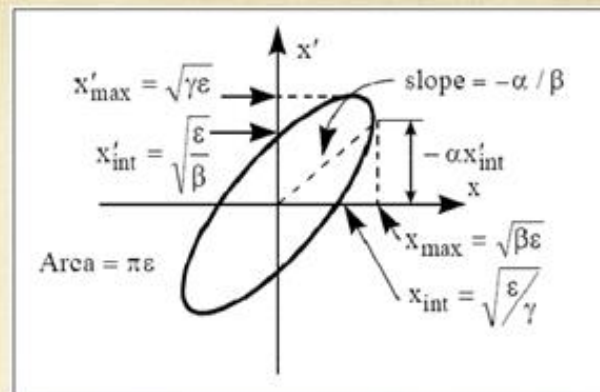
Refined scalings: C. Schroeder et al., PRSTAB 17, 101301, 2014, Y. Xi et al., PRSTAB 2013

→ **normalized emittance**
 ϵ_n down to 10^{-9} m rad

- Because the laser pulse intensity is **4 orders of magnitude** lower than in LWFA! $a_0=0.018$ instead of $a_0>1$
- Because the initial phase space volume is low
- Because the electrons are rapidly accelerated (space charge impact decreases as γ^{-2})
- Because initial ion shielding by released He ions

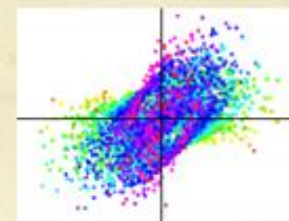
Ponderomotive force and phase mixing

Ponderomotive motion creates each ellipse.
Phase mixing overlaps all ellipses.



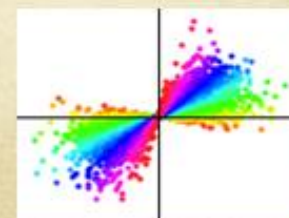
x direction (laser polarization)

Phase mixing + Ponderomotive motion



y direction

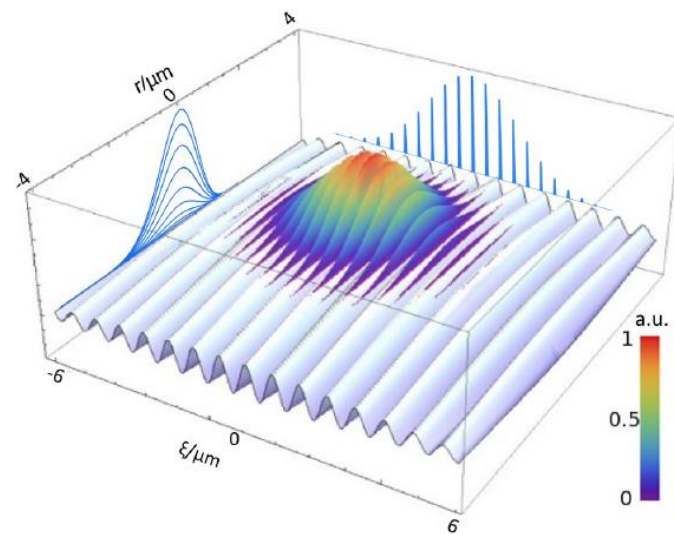
Phase mixing



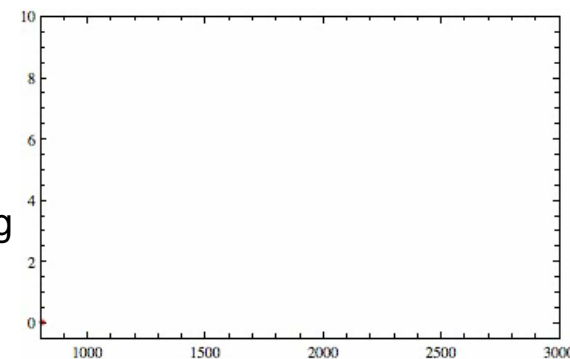
PIC simulation results d'accord with hybrid model

Y. Xi et al., PRSTAB, 2013

- Ionization based on ADK and YI (Yudin-Ivanov-model). G. L. Yudin and M. Y. Ivanov, *Phys. Rev. A*, 64:013409, 2001.
- Detailed numero-analytical analysis shows that $\varepsilon_{n,y}$ is about an order of magnitude lower, and increases slower than $\varepsilon_{n,x}$ as intensity increases. $\varepsilon_{n,y}$ down to the $\varepsilon_{n,y} \approx 10^{-9}$ m rad level or less.

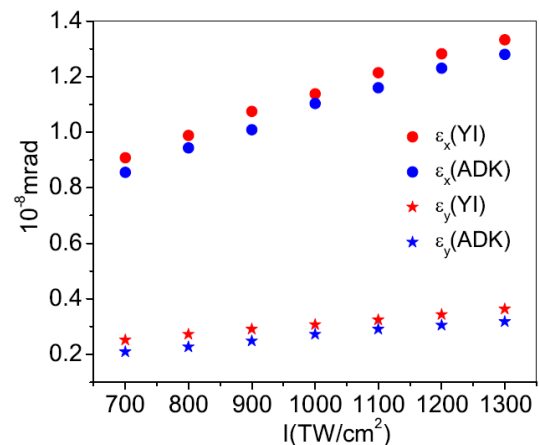
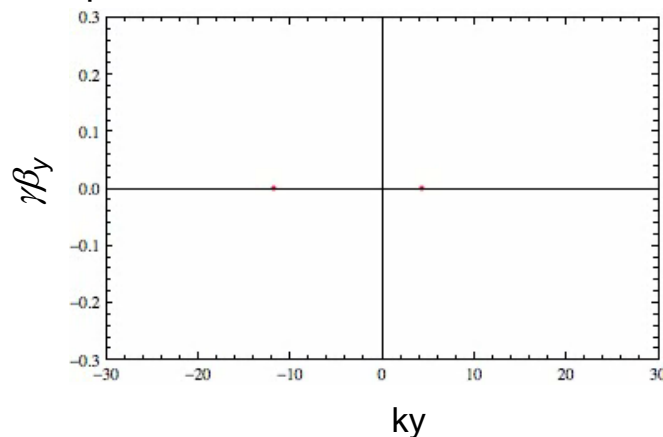
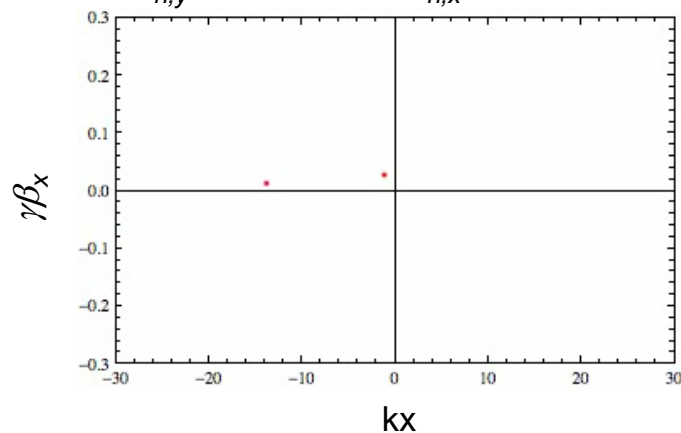


plasma velocity bunching



Laser linearly polarized in x-direction:

$\varepsilon_{n,y}$ smaller than $\varepsilon_{n,x}$ due to absence of ponderomotive motion



Similarities and differences of plasma photocathodes to rf photocathodes

	RF photoinjector	plasma photocathode
beam emittance sources	RF field	ponderomotive motion
	thermal effects	phase mixing
	space charge	space charge

residual momentum due to laser kick
electrons released at different betatron phases

$$\epsilon_{th} = \frac{w_0}{2} \sqrt{\frac{k_B T}{mc^2}}$$

approx. 0.5 mm mrad in standard photocathodes

In state-of-the-art rf photoguns, typically charges of 0.1-1 nC are released by lasers with spot sizes of the order of 1 mm. This leads to space charges 1-10 MV/m – a substantial fraction of the acc. field of ~100 MV/m. (J. Luiten, Int. J. Modern Physics A 22, 3882-3897, 2007)

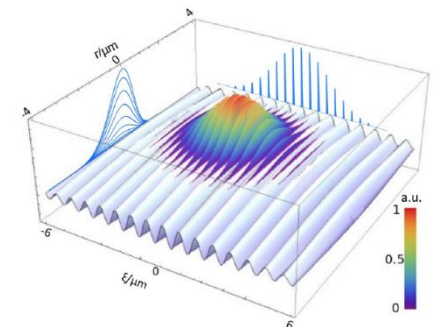
Acc. and focusing fields in plasma are two orders of magnitude larger!

- Tunability: Neglecting high laser frequencies, the released charge can be approximated by

$Q \propto \pi w_0^2 Z_R n_p \propto w_0^4$
Rough estimate when operating at ionization threshold: cylinder with Rayleigh length

$$N_e \approx n_{HIT} \sum_{(z_w - z_r)/c}^{(z_w + z_r)/c} T/2 \int \Gamma(x, y, \xi, t) dV$$

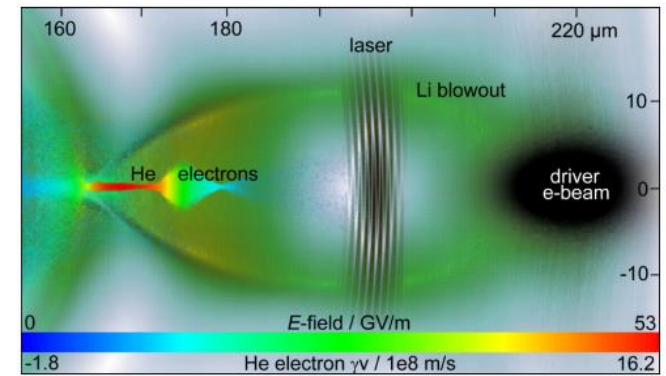
Exactly: integrated over ionization rates



Note that plasma density n_p (HIT) such as He, can be independently tunable of n_p (LIT) such as H!

Ultrahigh 5D brightness of TH mechanism

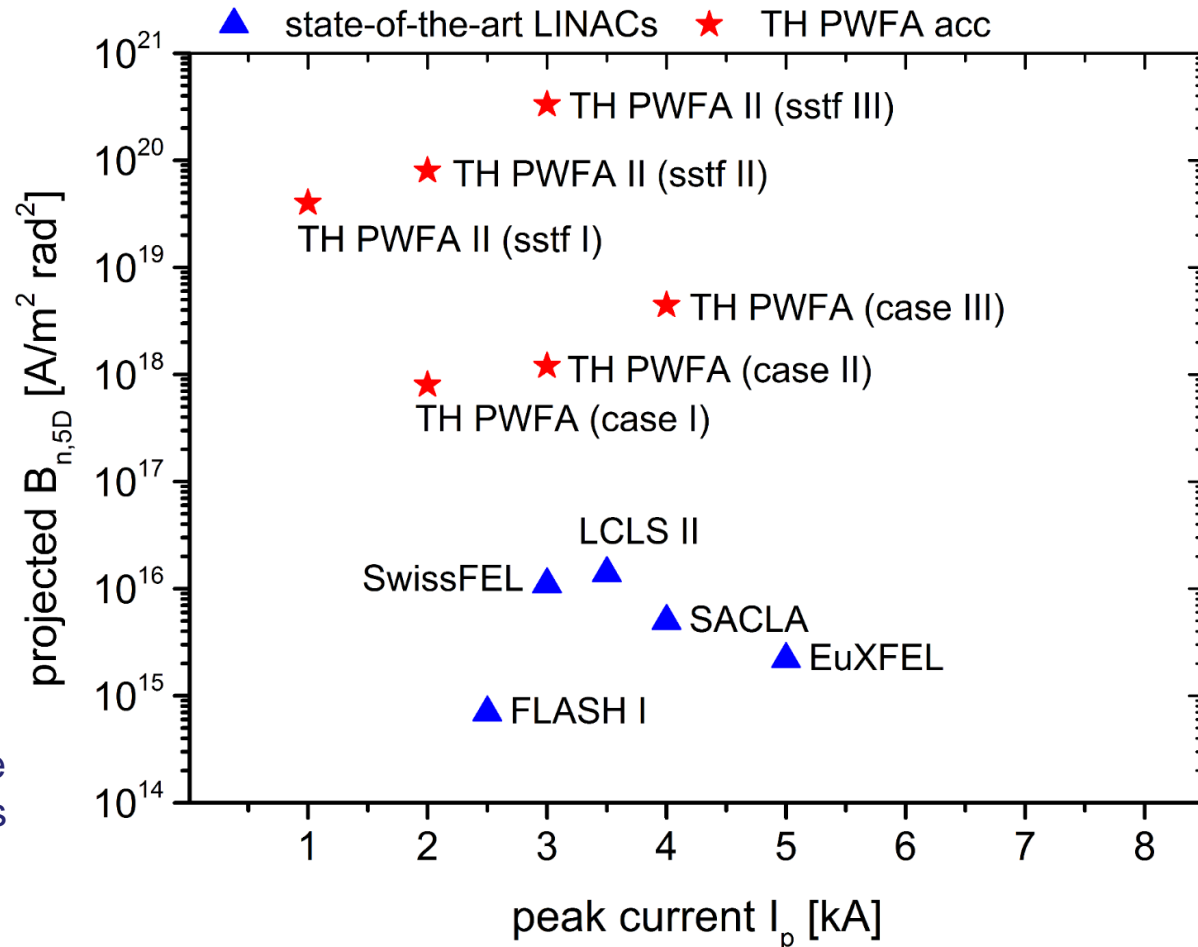
Ultracold electrons from plasma photocathode produce normalized emittance orders of magnitude lower than state-of-the-art



$$B = \frac{2I}{\epsilon_n^2}$$

⇒ Allows 5D brightness many orders of magnitude brighter than state-of-the-art

Emittance and brightness are key parameters which enable/determine performance in applications such as HEP (luminosity) or light sources (e.g. gain in FEL)



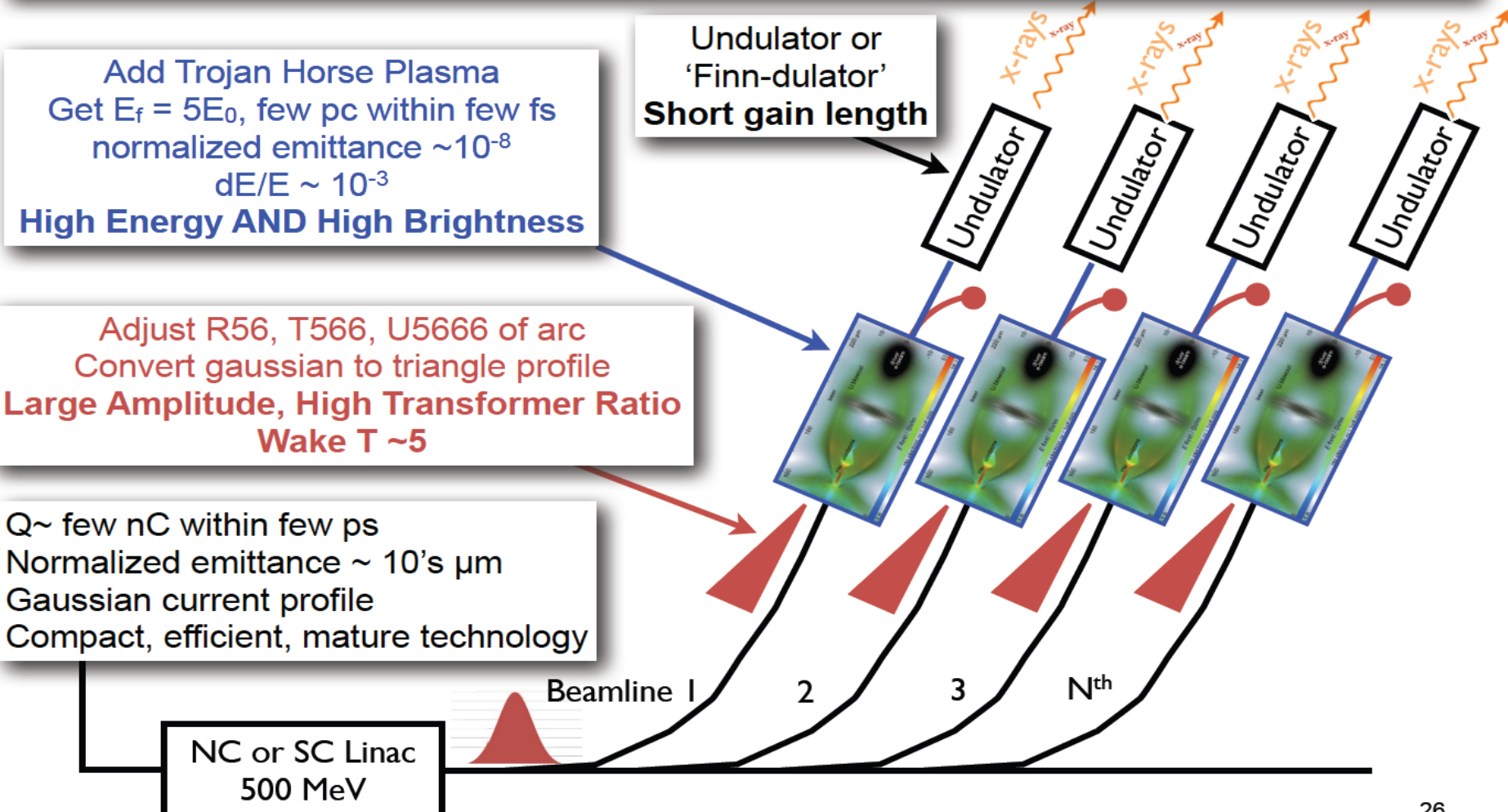
Hybrid Trojan Horse-based Future XFEL facility?

w/ M. Hogan (SLAC) et al., 5th Generation Light Source Workshop, 2013

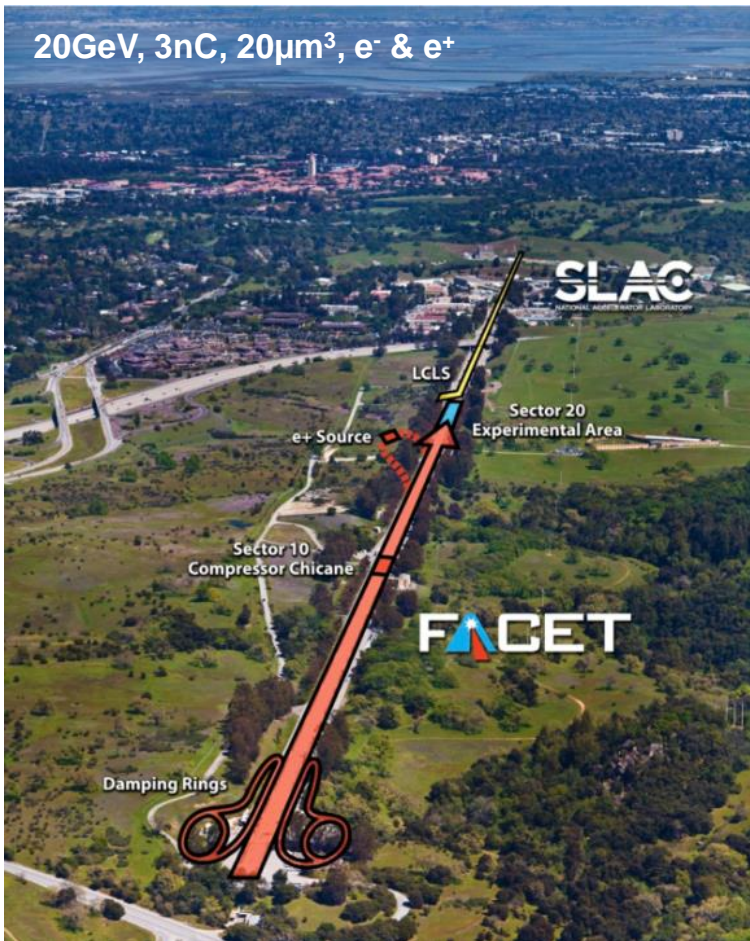
A Plasma Wakefield Accelerator Driven Compact X-FEL Plasma is Energy AND Brightness Transformer

SLAC

Compactness of plasmas accelerators, rep rate like rings with high brightness of linacs!



FACET – the premier facility for PWFA



Timeline:

- CD-0 2008
- CD-4 2012, Commissioning (2011)
- Experimental program (2012-2016)

“E210: Trojan Horse PWFA“ experiment approved in 2011

A National User Facility:

- Externally reviewed experimental program
- >200 Users, 25 experiments, 8 months/year operation

Key PWFA Milestones:

- ✓ Mono-energetic e⁻ acceleration
- ✓ High efficiency e⁻ acceleration (*Nature* **515**, Nov. 2014)
- ✓ First high-gradient e⁺ PWFA (*Nature* **524**, Aug. 2015)

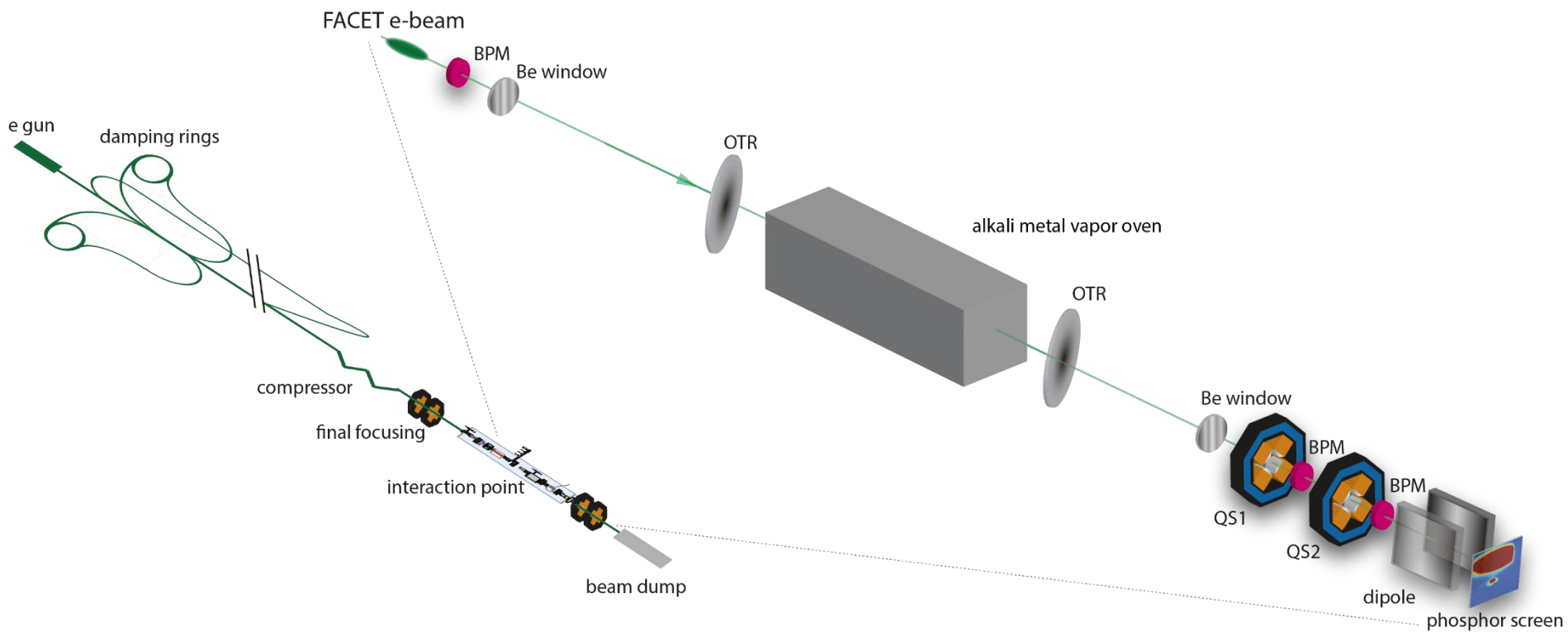
E210: Multi-institutional, cross-continental collaboration of academia (Strathclyde—UCLA—Hamburg—Oslo—Texas—Boulder), research centers (SLAC—DESY) and industry (RadiaBeam—Tech-X—Radiasoft)

PI's B. Hidding (Strathclyde) & J.B. Rosenzweig (UCLA)

2012-2017, experiments at FACET ramping up from 2013-2016

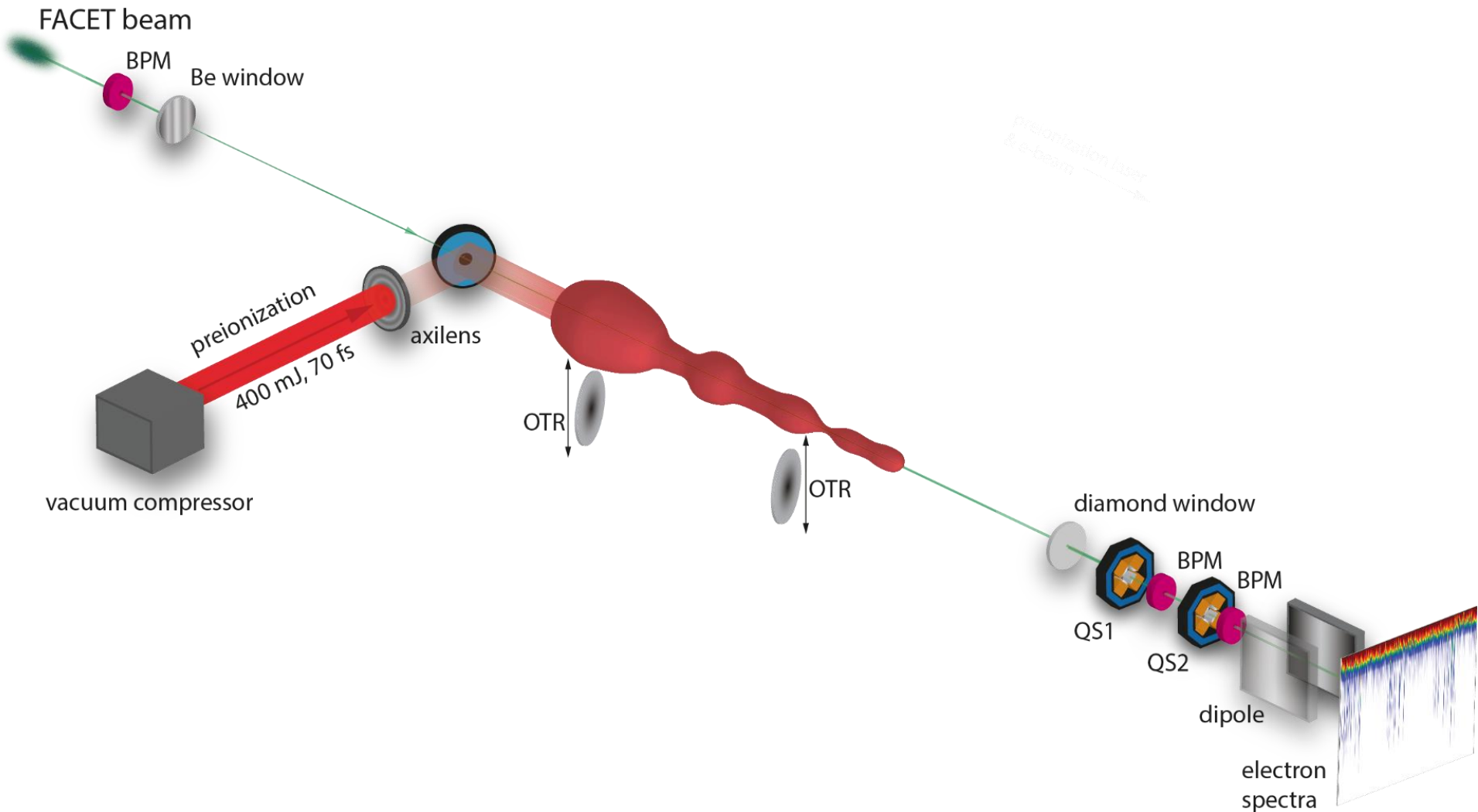
Supported e.g. by Beam Brightness Transformer for Laser-Wakefield Accelerators DOE R&D program, RadiaBeam Technologies 2012-2016, EuPRAXIA WP14 etc.

2012 at FACET: use hot alkali metal vapor, self-ionized by driver beam



2013/14:

Ti:Sapphire commissioning, optical pre-ionization of (noble) gas



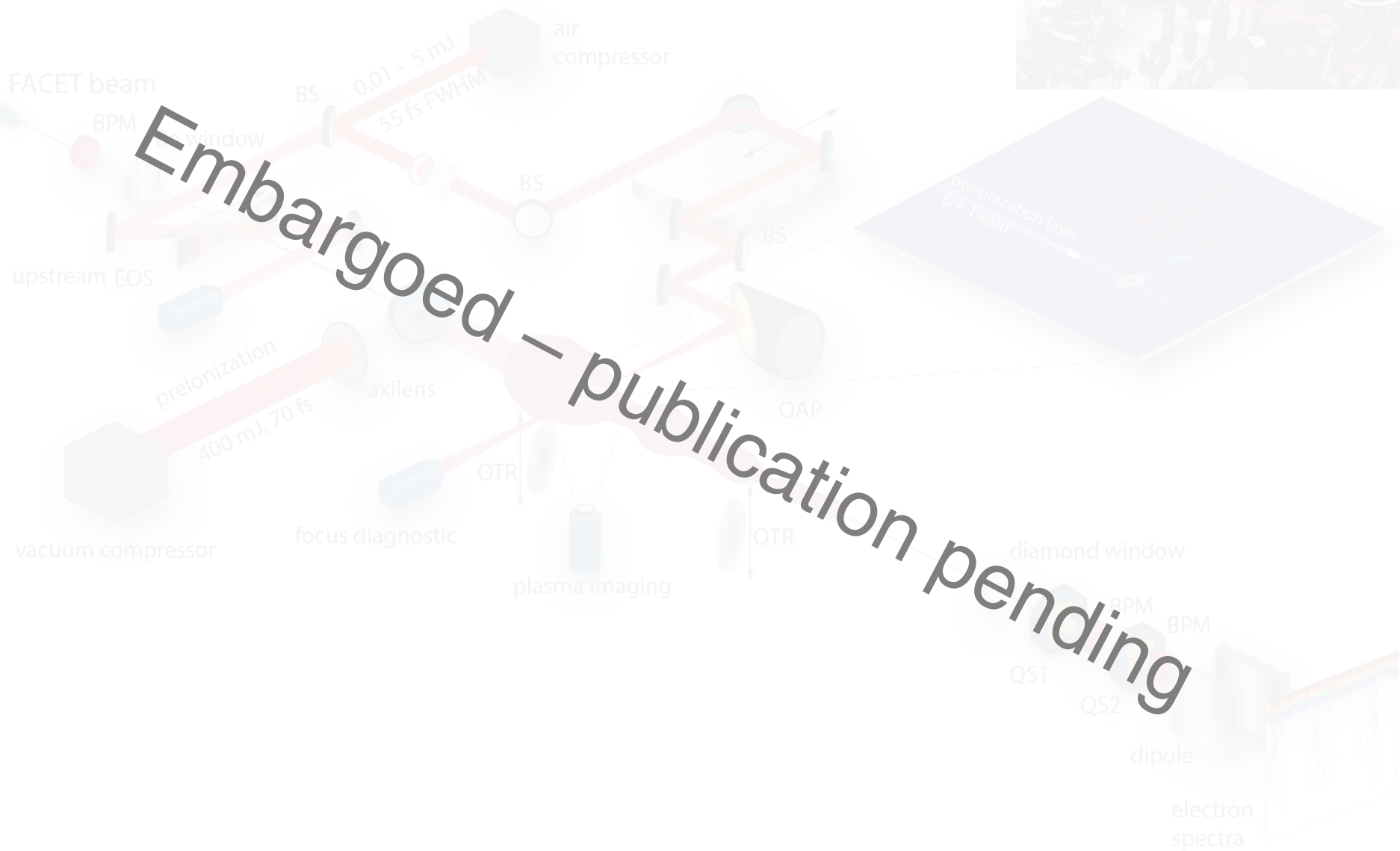
2013/14:

Commissioning of electro-optical sampling based time-of-arrival diagnostics, separate air compressor to allow for independently tunable beams



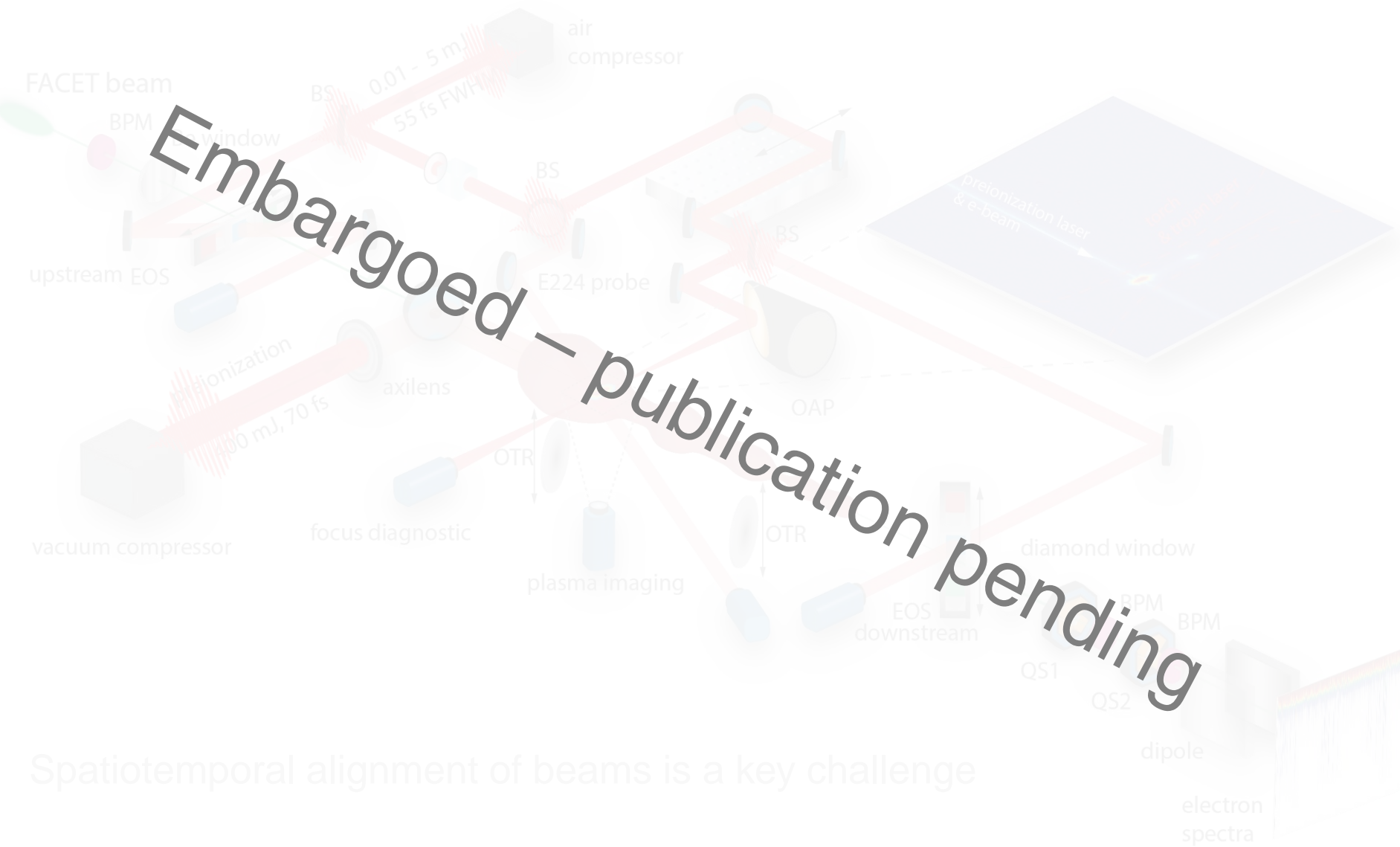
Embargoed – publication pending

2015: Add Trojan Horse plasma photocathode laser
(in 90° geometry)



Embargoed – publication pending

2016: Full E210 setup with two independently tunable main laser arms, up to 5 laser beams (1 preionization, 2 EOS, 1 Trojan photocathode, 1 E224 probing) from vacuum and air compressor, and SLAC linac electron beam



Embargoed – publication pending

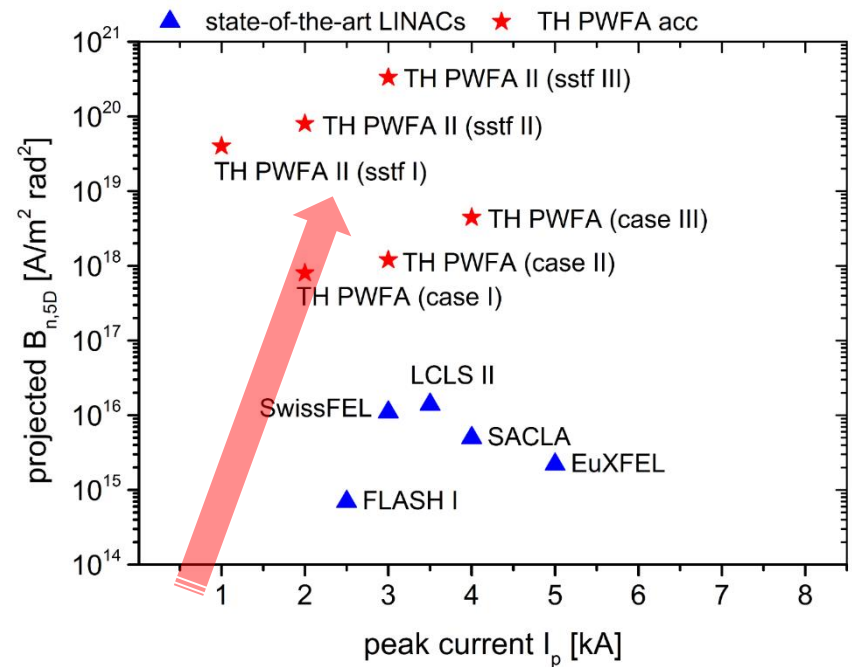
Spatiotemporal alignment of beams is a key challenge

Spatiotemporal alignment of beams is a key challenge:
Preionization laser pulse and electron beam

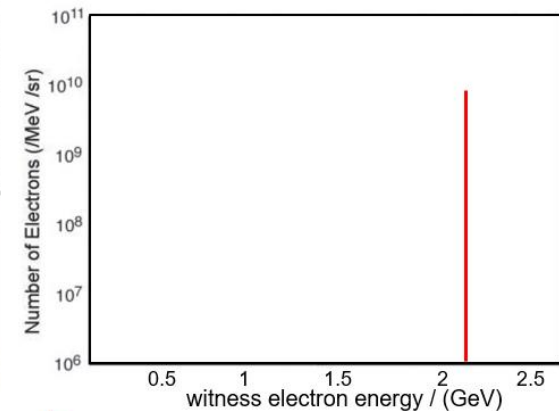
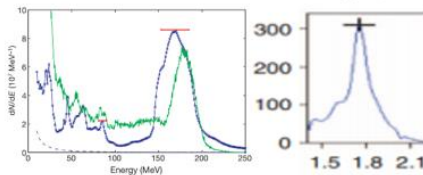
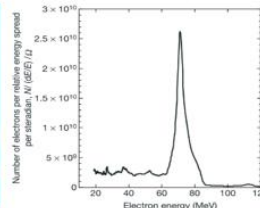
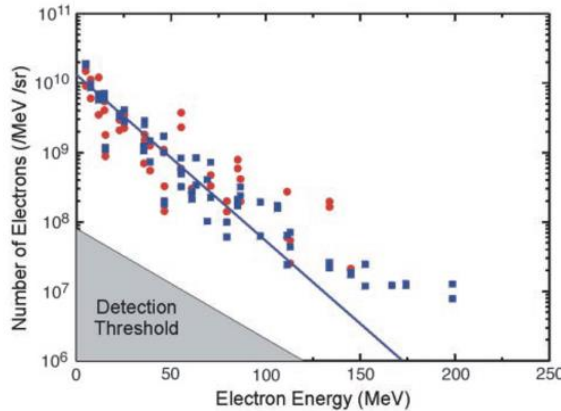


The energy spread challenge

Prospect for tunable bunches with ultralow emittance and ultrahigh 5D-brightness is great, but



Energy spread is a big problem, can be showstopper for FEL, for example. New approach to reduce energy spread by two orders of magnitude is needed!

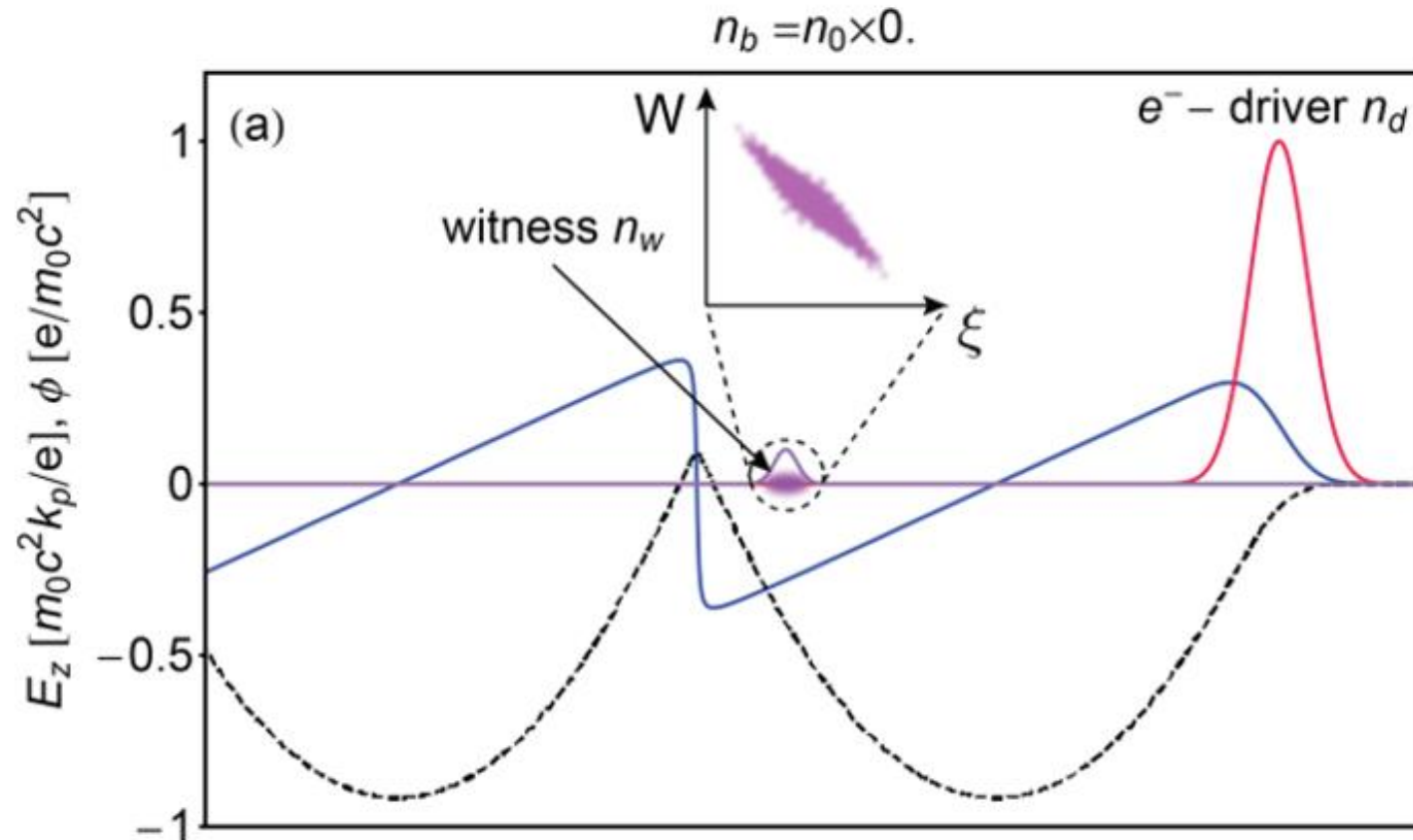


exponential spectra, pre 2004

quasimonoeenergetic beams, 2004 - today

NeXSource: relative energy spreads < 0.01%

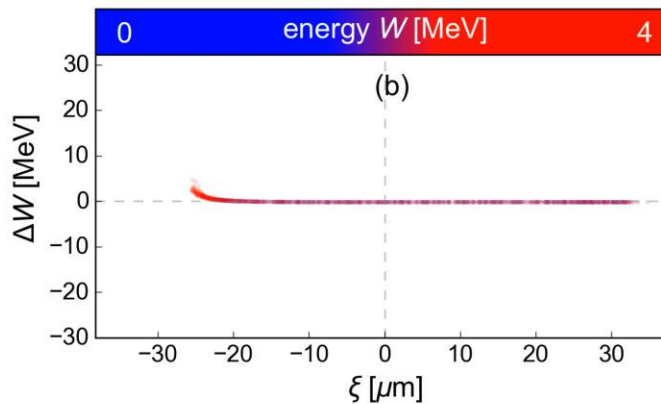
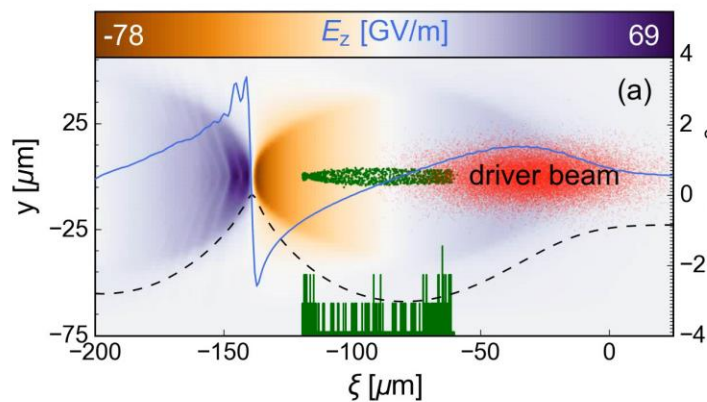
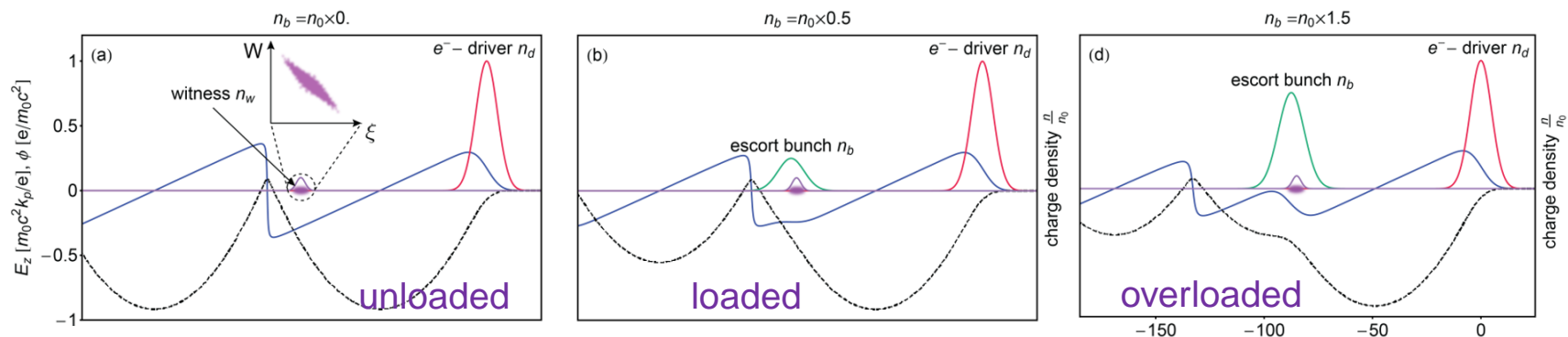
Path is open to ultralow TH emittance and ultrahigh 5D-brightness, but energy spread may destroy beam quality during extraction & transport
⇒ showstopper e.g. for FEL



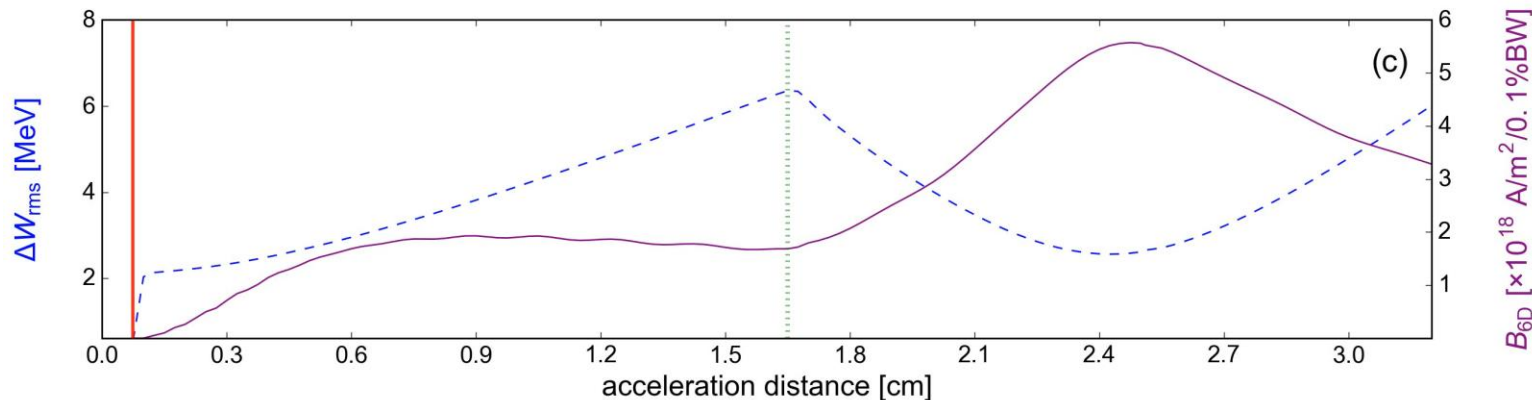
“the energy spread&chirp problem“:
‘steep’ price to be paid for ultrahigh energy gradients.
How to get rid of energy chirp/spread, how to generate ultrahigh 6D brightness bunches?

Concept of TH-released “escort beam” for chirp control

Tailored beam loading via escort bunch allows chirp control:

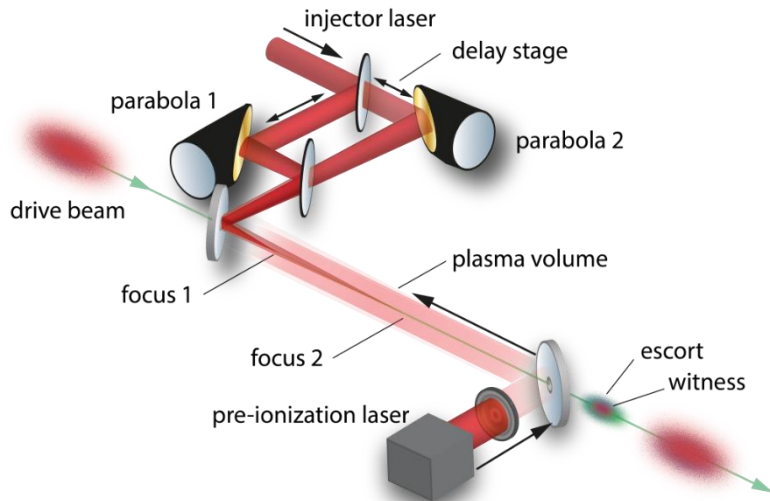


VSim

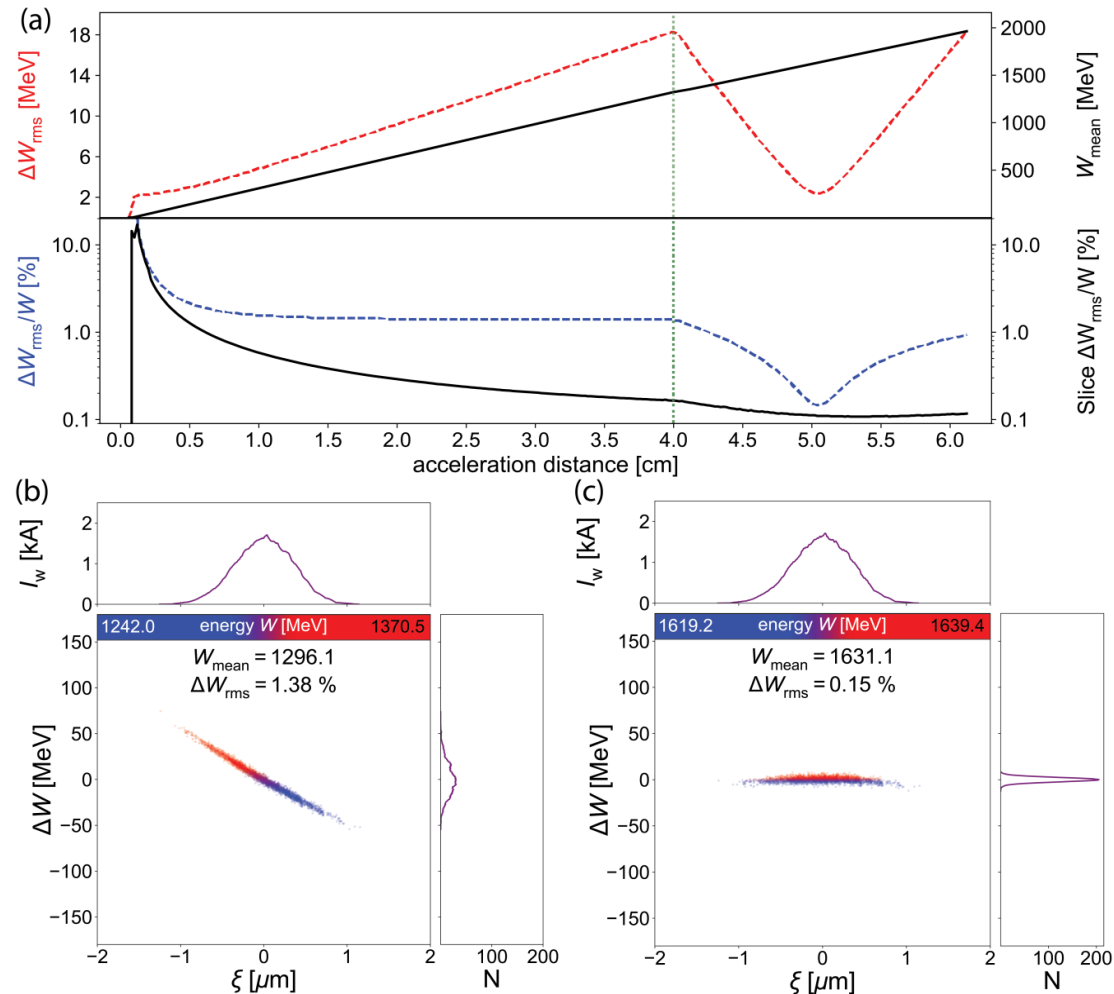


Energy and energy spread control

Works at any energy:



	Before dechirping	After dechirping
z_{acc}	14.8 cm	22.9 cm
Q	8 pC	8 pC
σ_z	2.6 μm	2.6 μm
I_{peak}	2.0 kA	2.0 kA
\overline{E}	922 MeV	1404.3 MeV
σ_E	1.12 %	0.033 %
ϵ_n	40 nm · rad	43 nm · rad



Residual energy spread scaling

Residual energy scaling:

$$\Delta W_{\text{res,max}} = 2 E_{z,\text{trap}} Z_R$$

Generalized:

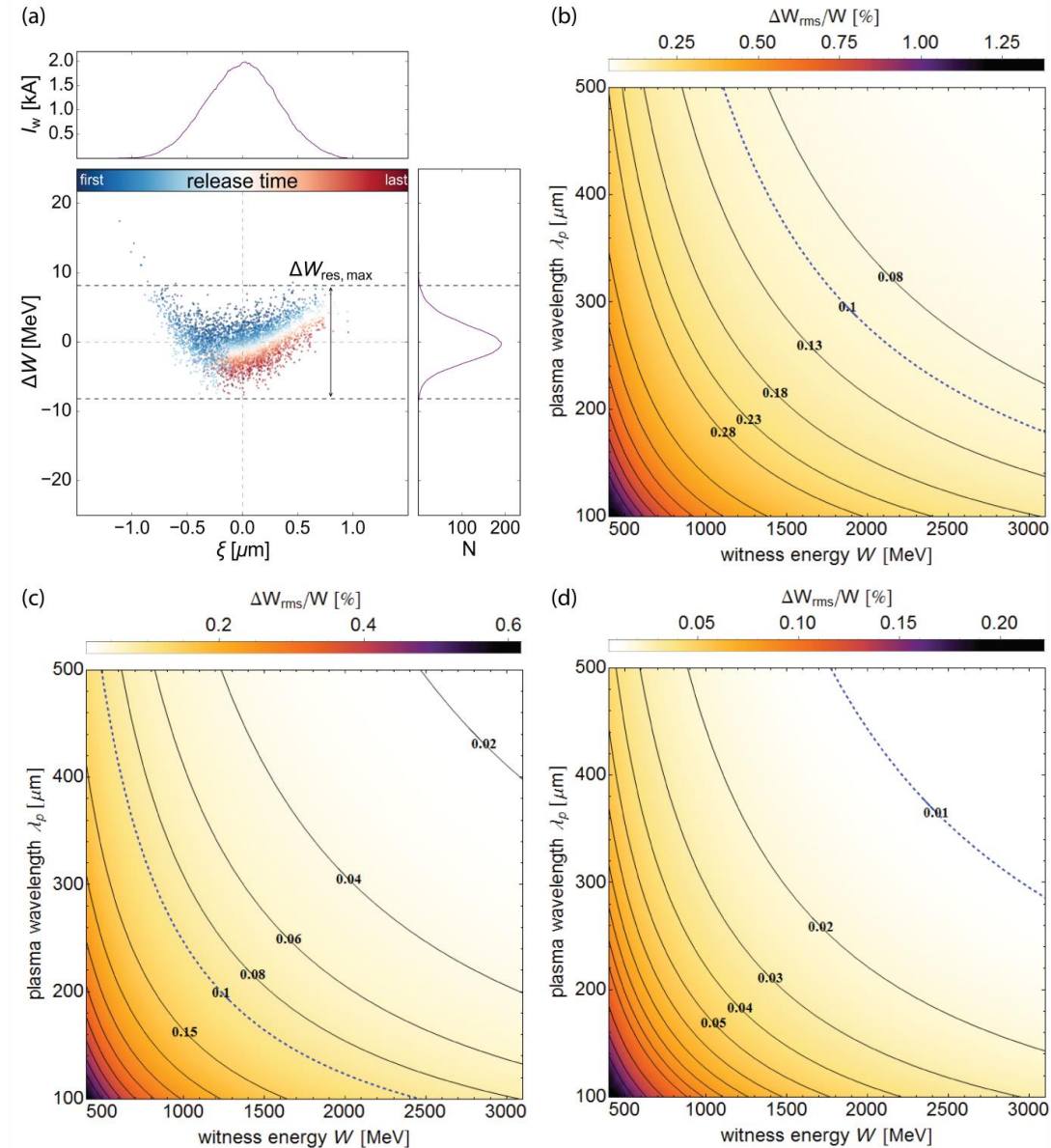
$$\Delta W_{\text{res,max}} \approx 2\pi/5 E_{z,\text{trap}} w_{0,w}^2 / \lambda_L$$

$$\approx 96 n_0^{1/2} [\text{cm}^{-3}] 2\pi/5 w_{0,w}^2 / \lambda_L$$

The residual energy spread scaling suggests the use of low plasma (LIT) densities.

Similar trend as in LWFA (energy gain vs. dephasing), but for completely different reasons

$$\Delta W_{\text{res,rms}} \approx \Delta W_{\text{res,max}} / 5 \approx 2/5 E_{z,\text{trap}} Z_R \approx 2\pi/5 E_{z,\text{trap}} w_0^2 / \lambda_L$$

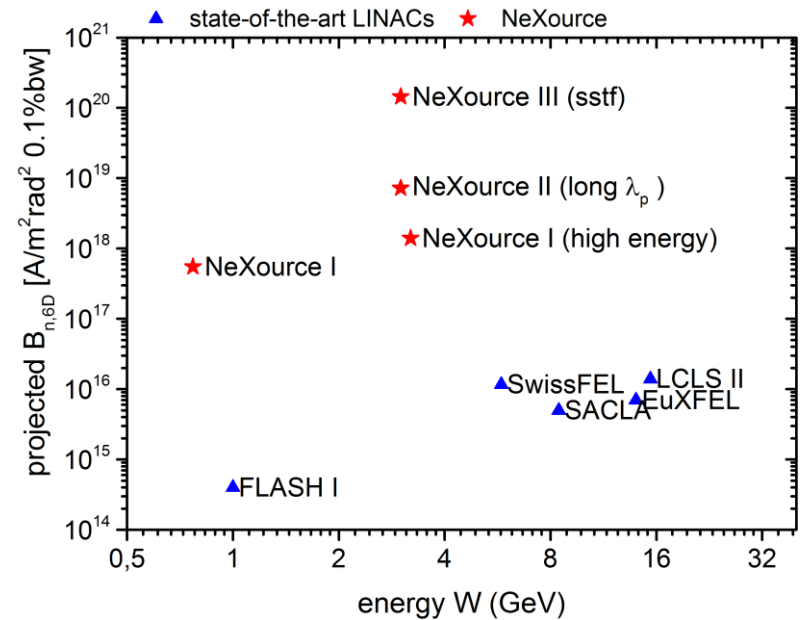


Ultrahigh 6D brightness

Emittance & brightness and energy spread is combined into 6D brightness:

$$B_{n,6D} = \frac{I_p}{\epsilon_{n,x} \epsilon_{n,y} 0.1\% \sigma_W}$$

Comparison with state-of-the-art accelerator systems reveals increase by orders of magnitude of 6D brightness!



Intense Electron Source



Trojan Horse / NeXource

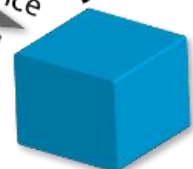
plasma photocathode: emittance, brightness, energy, energy spread & stability transformer

Photon Science



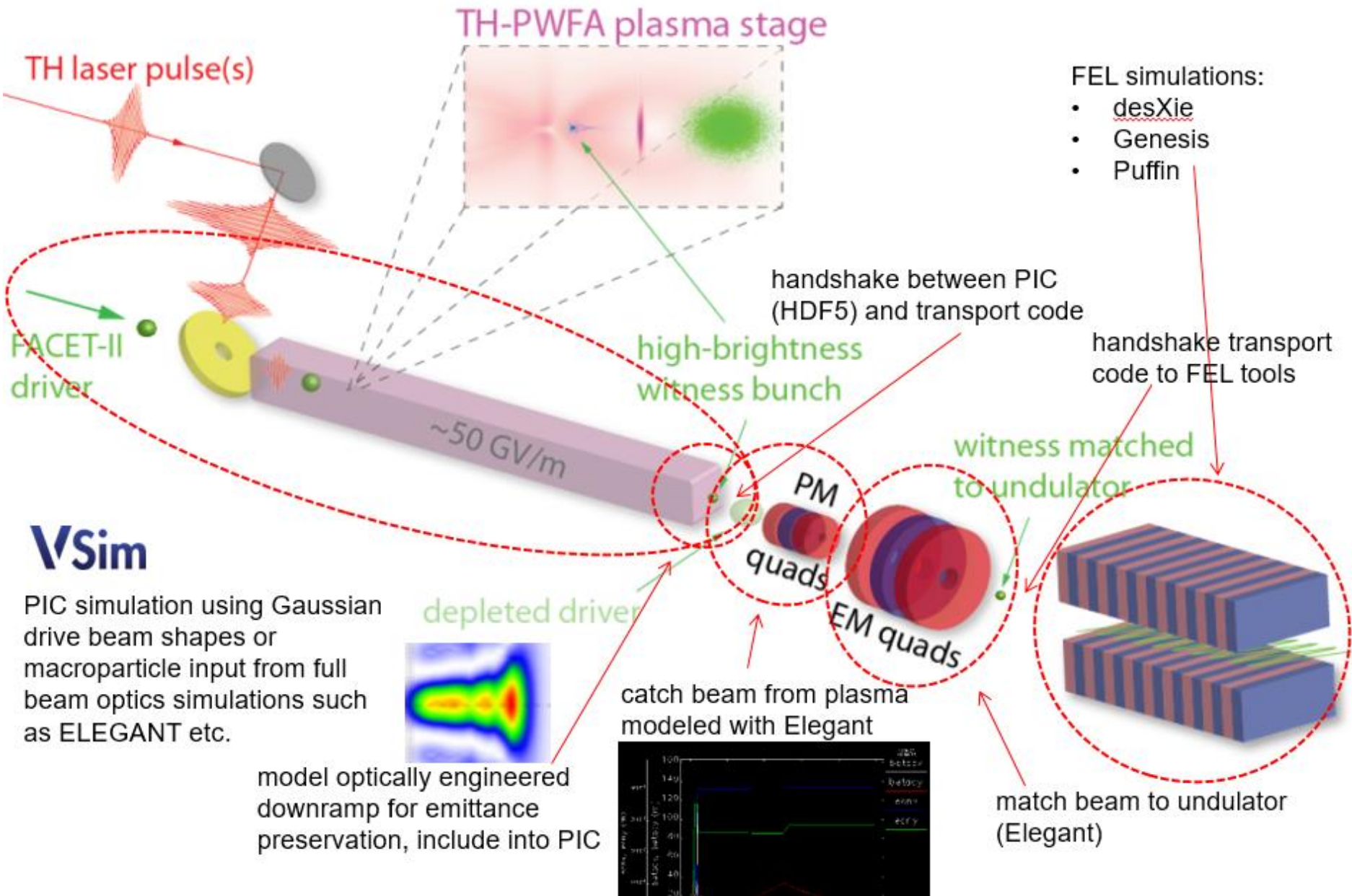
e.g. boost FEL gain, ultrashort γ -pulses, multicolor beams...

High Energy Physics



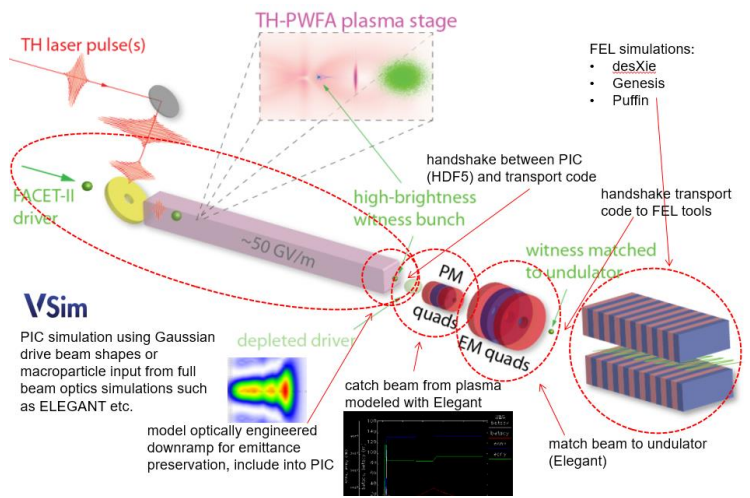
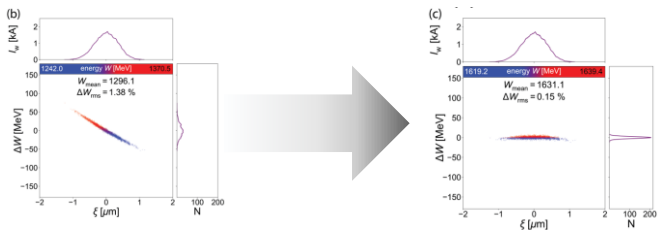
e.g. as injector, staging..

Photon science: FEL



Energy spread compensation and ultrahigh 6D brightness: NeXource project

- TH mechanism for ultralow emittance and unprecedented 5D-brightness
- However, substantial correlated energy spread (chirp) is side-effect of GV/m fields
- New chirp compensation technique *NeXource* allows to remove correlated energy spread and generate ultrahigh 6D-brightness beams (reduction of energy spread by 2 orders of magnitude)



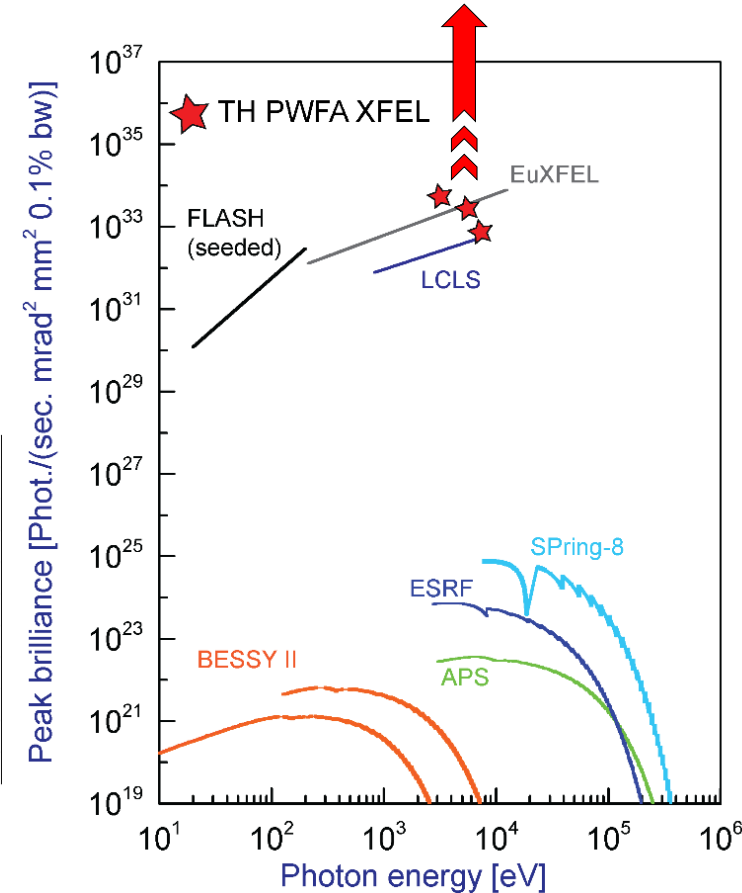
- This is a key step towards key applications such as 5th generation light sources
- E.g. for the race towards plasma-based FEL which is a main driver in the worldwide community: Beat Pierce parameter, fulfil Pellegrini criterion, and harness ultrahigh gain to realise compact hard x-ray FELs

$$\epsilon_n < \lambda_r \langle \gamma \rangle / 4\pi \quad \checkmark \quad \langle \sigma_\gamma / \gamma \rangle \ll \rho \quad \checkmark \quad L_{g,1D} = \frac{\lambda_u}{4\pi\sqrt{3}\rho_{1D}} \propto B_e^{-1/3}$$

- Preliminary start-to-end simulations look extremely exciting

Ultra-high 6D-brightness: enabling 5th generation light sources

preliminary start-to-end simulations:



Embargoed –
publication pending

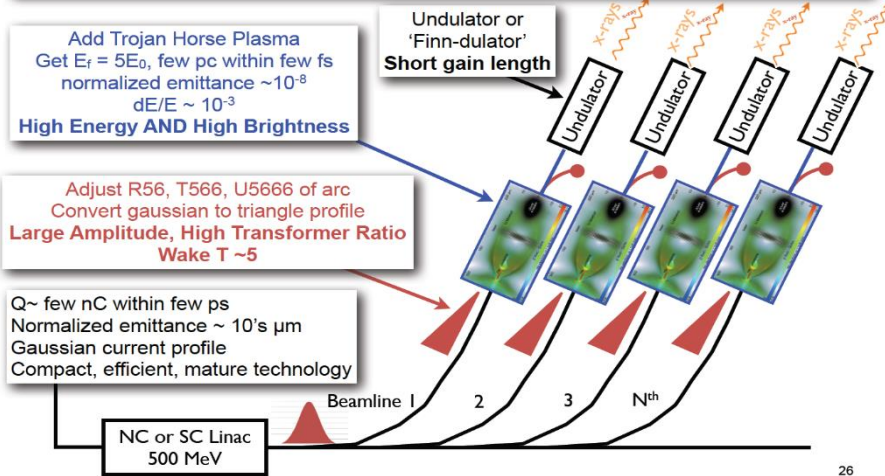
**4.45 angstrom, bandwidth ~ 0.1% , saturation power 35 GW
FWHM pulse duration sub-fs**

Make concept compact: Use LWFA output for PWFA

A Plasma Wakefield Accelerator Driven Compact X-FEL Plasma is Energy AND Brightness Transformer

SLAC

Compactness of plasmas accelerators, rep rate like rings with high brightness of linacs!

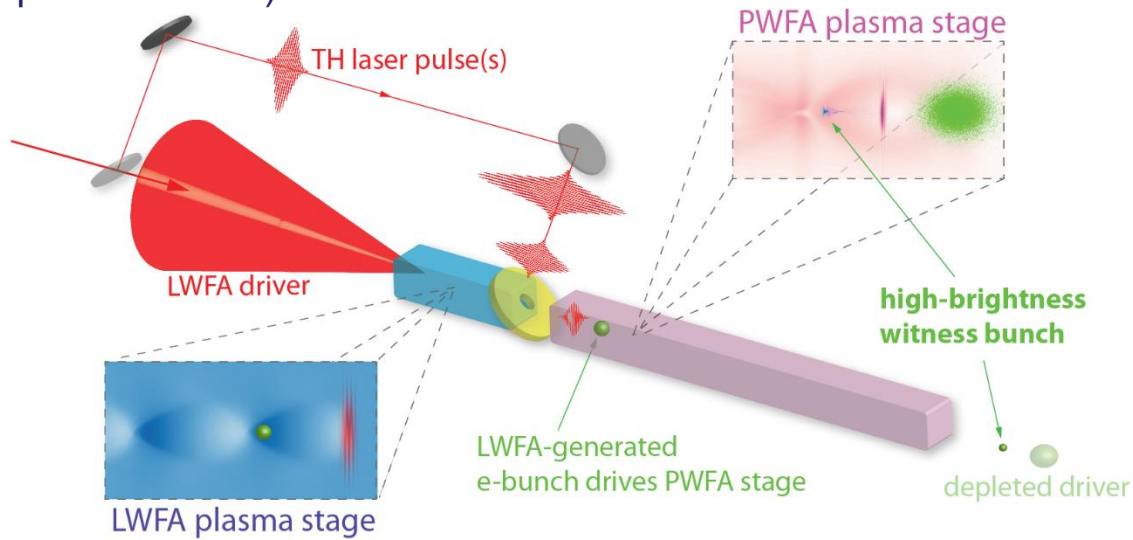


500 MeV linac: Still big machine

EuPRAXIA

NOVEL FUNDAMENTAL RESEARCH
COMPACT EUROPEAN PLASMA
ACCELERATOR WITH SUPERIOR
BEAM QUALITY

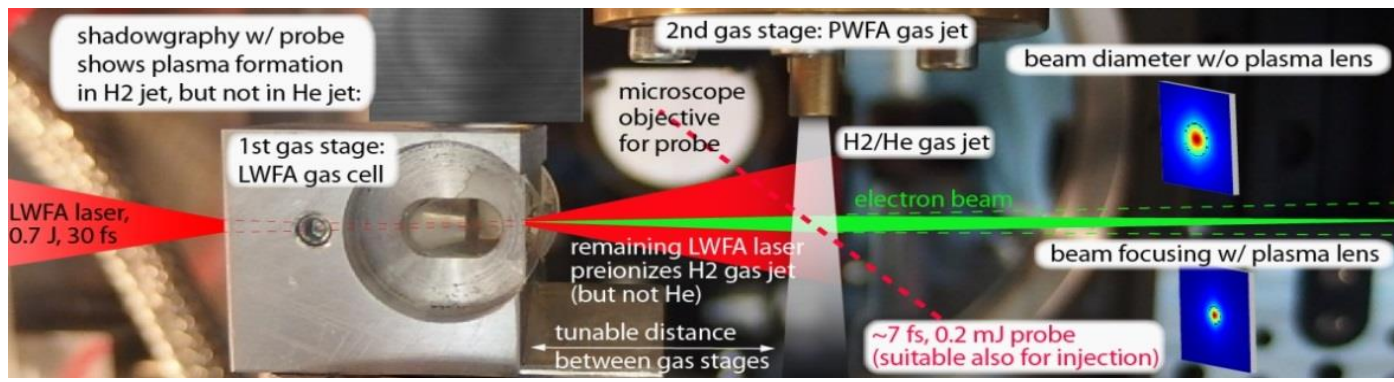
Compact option for EuPRAXIA: generate PWFA driver beams via LWFA (and then spike it with TH)



Make concept compact: Use LWFA output for PWFA

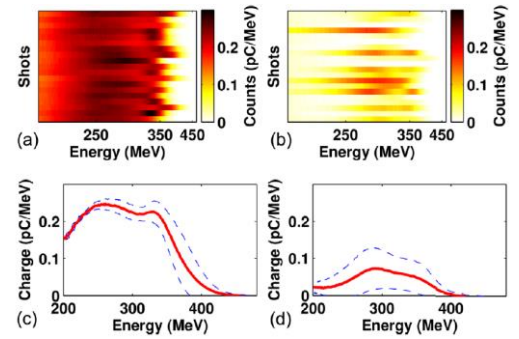
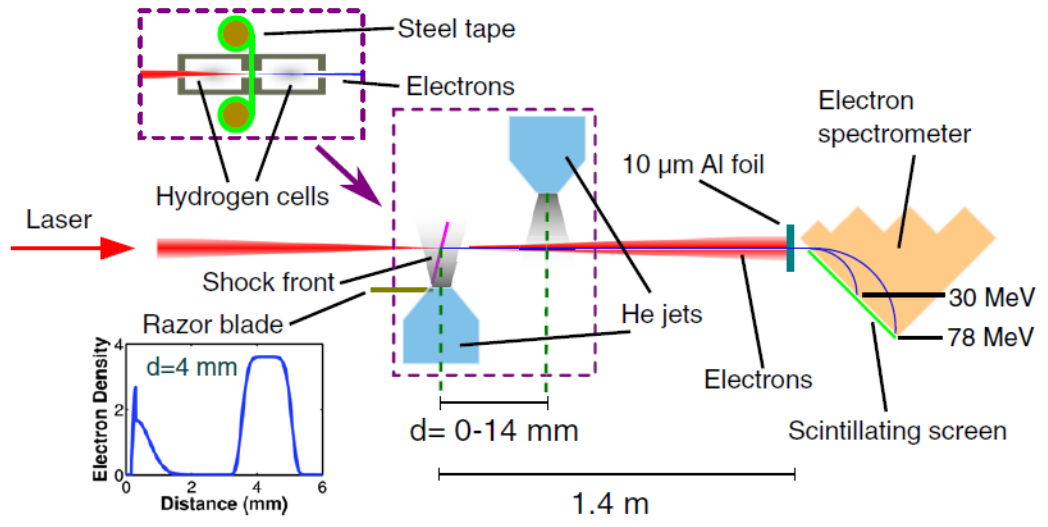


“Hybrid energy doubling”
PRL 104, 195002, 2010



Experiments FSU Jena: use laser remnant from LWFA stage to preionize H2, but not He in PWFA stage (i.e. 2nd gas jet), Kuschel et al: PRAB 2016

Joint WP14 campaign(s) at HZDR Dresden, promising results as regards plasma lensing and bunch deceleration

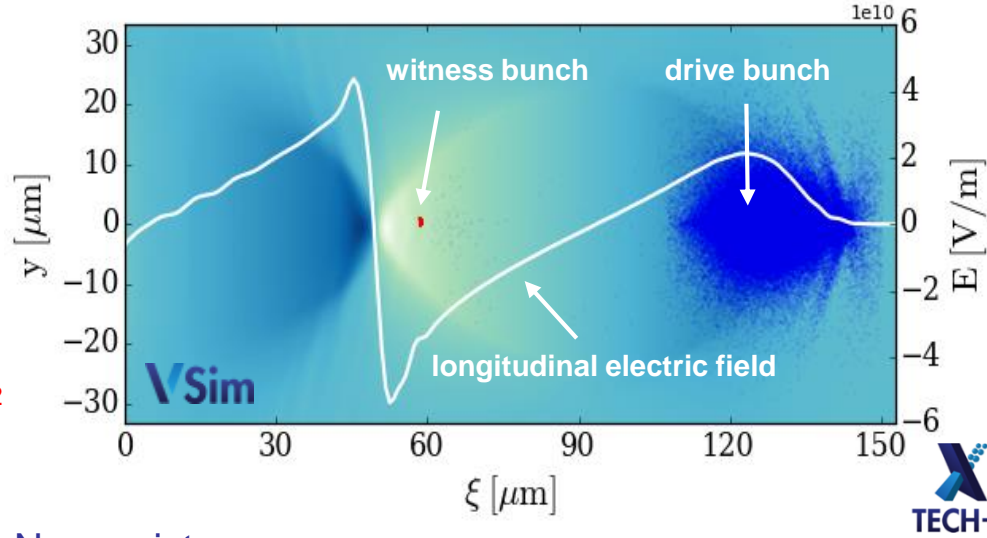


Chou.. Karsch et al., “Collective deceleration“, PRL 2016

Beam quality transformation and stabilization

Witness:

$\sigma_x \approx \sigma_y \approx \sigma_z \approx 0.6 \mu\text{m}$
 $Q \approx 7.3 \text{ pC}$
 $\gamma \approx 610$ after $\approx 9 \text{ mm}$
 $\Delta\gamma/\gamma \approx 2.5\%$
 $\varepsilon_n \approx 2.4 \times 10^{-8} \text{ mrad}$
 $B_{5D} \approx 3.7 \times 10^{19} \text{ A/m}^2\text{rad}^2$



Driver:

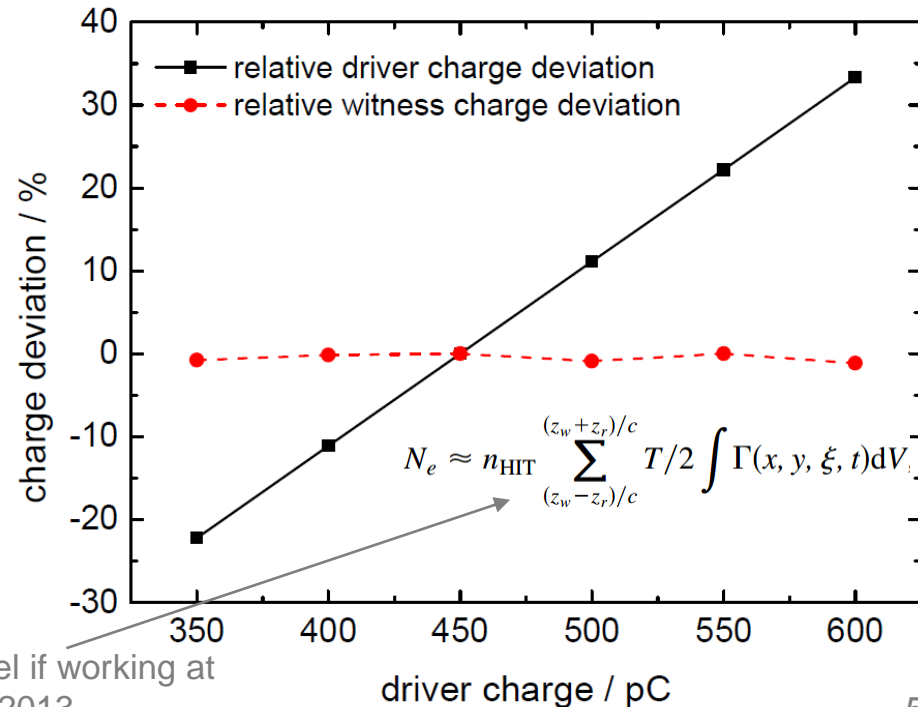
$\sigma_x = \sigma_y = \sigma_z = 7 \mu\text{m}$
 $Q = 400 \text{ to } 600 \text{ pC}$
 $\gamma = 500 \text{ to } 2000$
 $\Delta\gamma/\gamma = 10\% \text{ to } 40\%$
 $\varepsilon_n = 2.25 \times 10^{-6} \text{ mrad}$

preionized Hydrogen-Neon mixture:

LIT: H and Ne @ $n_e = 1.5 \times 10^{17} \text{ cm}^{-3}$
 HIT: Ne⁺ @ $n_e = 9 \times 10^{16} \text{ cm}^{-3}$

TH laser: $a_0 = 0.041$, $w_0 = 5 \mu\text{m}$, $\tau = 25 \text{ fs}$,
 $\lambda = 800 \text{ nm}$

- Excellent trapped witness charge stability < 1%, independent of drive beam over 350-600 pC range



need to take into account MPI via Yudin-Ivanov model if working at elevated laser frequencies, see, Y. Xi et al, PRSTAB 2013

Witness energy and $\Delta\gamma/\gamma$ resilience vs. jitter of driver energy and spread

Witness:

$$\sigma_x \approx \sigma_y \approx \sigma_z \approx 0.6 \mu\text{m}$$

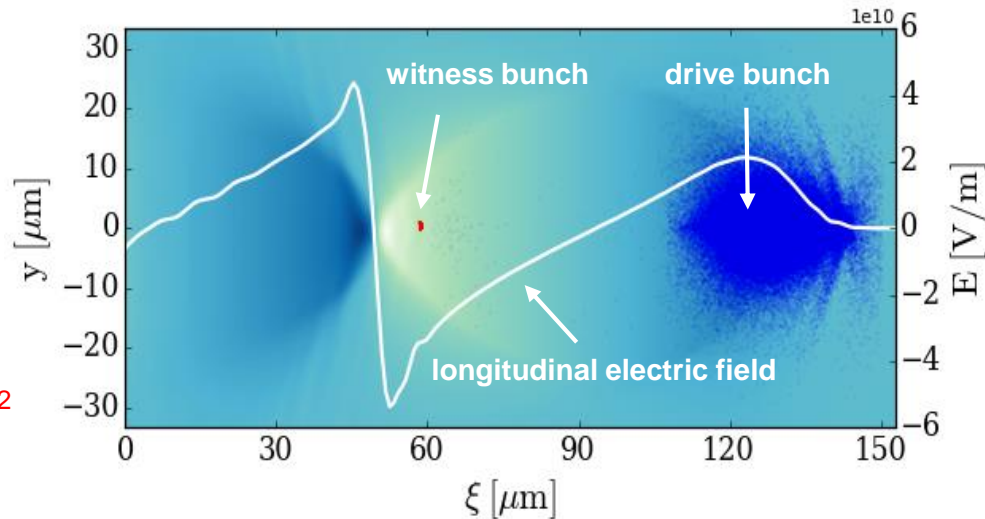
$$Q \approx 7.3 \text{ pC}$$

$$\gamma \approx 610 \text{ after } \approx 9 \text{ mm}$$

$$\Delta\gamma/\gamma \approx 2.5\%$$

$$\varepsilon_n \approx 2.4 \times 10^{-8} \text{ mrad}$$

$$B_{5D} \approx 3.7 \times 10^{-19} \text{ A/m}^2\text{rad}^2$$



Driver:

$$\sigma_x = \sigma_y = \sigma_z = 7 \mu\text{m}$$

$$Q = 400 \text{ to } 600 \text{ pC}$$

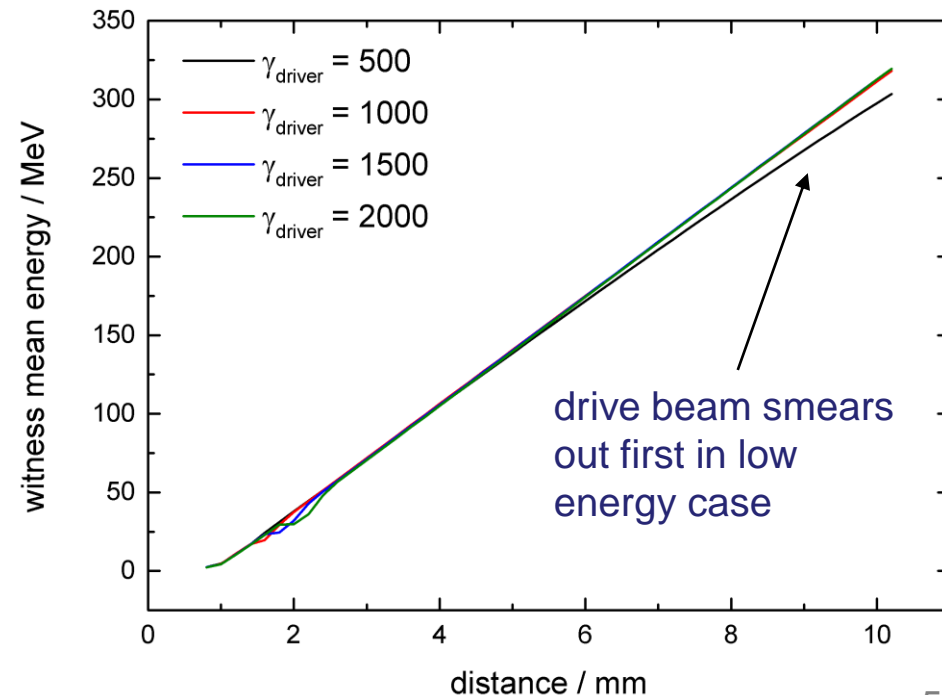
$$\gamma = 500 \text{ to } 2000$$

$$\Delta\gamma/\gamma = 10\% \text{ to } 40\%$$

$$\varepsilon_n = 2.25 \times 10^{-6} \text{ mrad}$$

- Drive beam electron energy varied from $E = 250\text{-}1000 \text{ MeV}$ (conservative choice given that $4 \text{ GeV}+$ has already been reached in experiments)
- Witness energy stable on (sub) %-level, only 250 MeV driver case leads to reduced final energy. Need to cap plasma at desired working point (trade-off energy stability vs. max. energy)
- Reason combination of depletion and driver beam longitudinal lengthening

witness energy for different driver energies



Witness energy and $\Delta\gamma/\gamma$ resilience vs. jitter of driver energy and spread

Witness:

$$\sigma_x \approx \sigma_y \approx \sigma_z \approx 0.6 \mu\text{m}$$

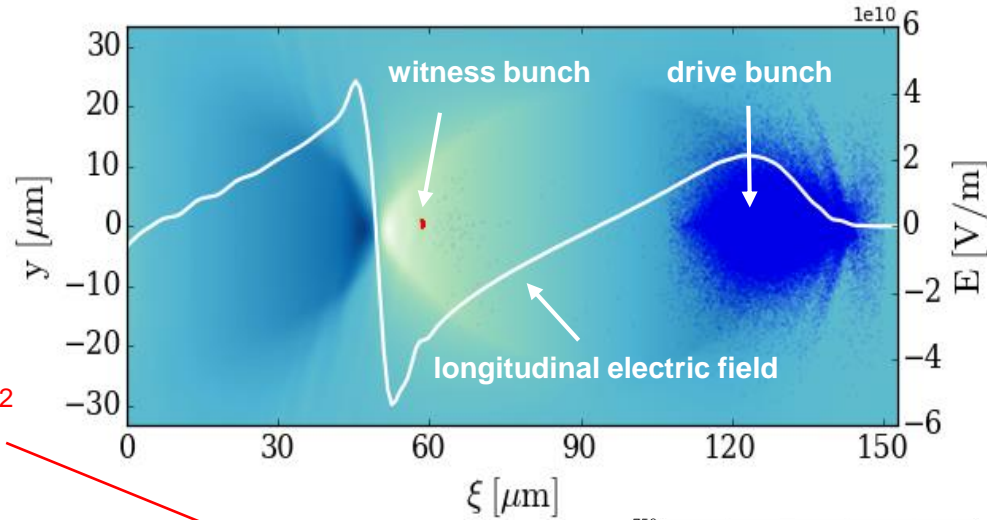
$$Q \approx 7.3 \text{ pC}$$

$$\gamma \approx 610 \text{ after } \approx 9 \text{ mm}$$

$$\Delta\gamma/\gamma \approx 2.5\%$$

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$$B_{5D} \approx 3.7 \times 10^{-19} \text{ A/m}^2\text{rad}^2$$



Driver:

$$\sigma_x = \sigma_y = \sigma_z = 7 \mu\text{m}$$

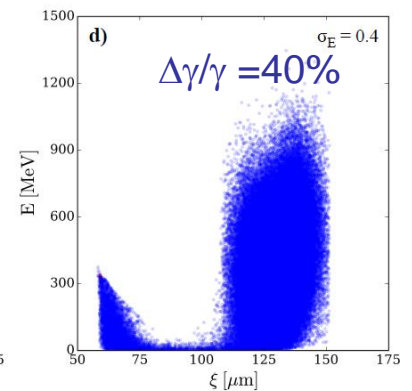
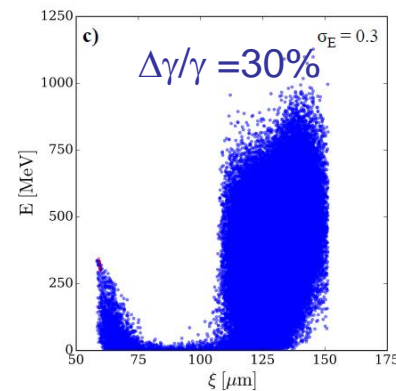
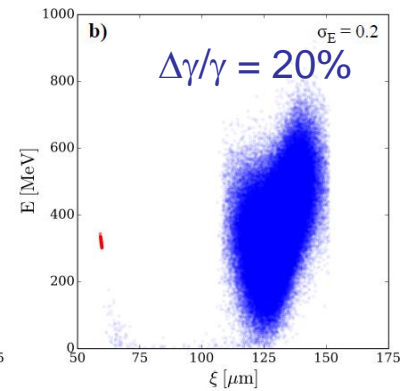
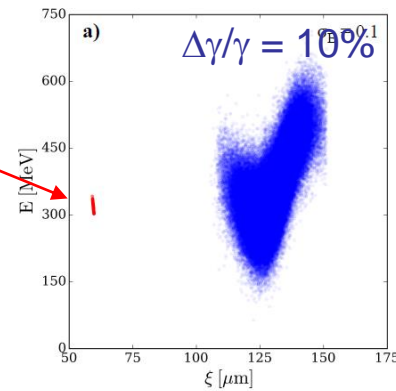
$$Q = 400 \text{ to } 600 \text{ pC}$$

$$\gamma = 500 \text{ to } 2000$$

$$\Delta\gamma/\gamma = 10\% \text{ to } 40\%$$

$$\varepsilon_n = 2.25 \times 10^{-6} \text{ mrad}$$

- Energy spread $\sim 2.5\%$ in all cases, even if driver has $\Delta\gamma/\gamma$ of tens of % (here: uncorrelated)
- Note: this is the low energy limiting $\gamma=500$ case, at higher energies driver degradation is reduced and stability and energy gain is increased



..to be published

Summary

- Hybrid plasma acceleration: make the best out of two worlds and combine LWFA and PWFA features
- Use Trojan Horse plasma photocathode method to produce controllable bunches with emittance and 5D-brightness orders of magnitude better than state-of-the-art (first successful experiments at SLAC FACET)
- Combine Trojan Horse technique with dechirper and produce 6D brightness beams orders of magnitude better, beat Pellegrini, Pierce at same time (theory but doability easier than Trojan Horse). No experiments yet



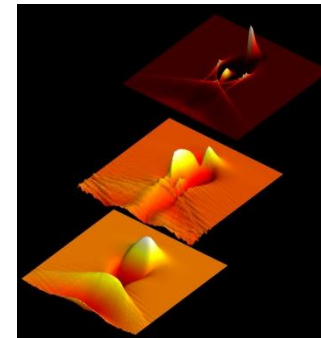
- Use LWFA output (high current etc.) for driving PWFA's and make system really compact (first encouraging experiments)



Backup

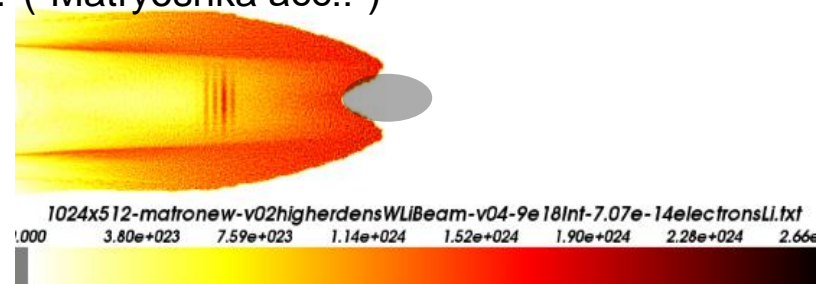
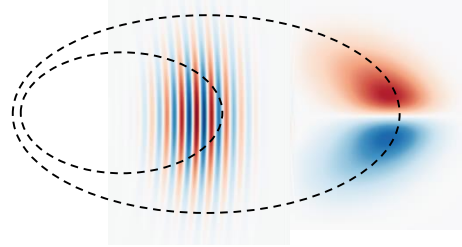
Take the best of both worlds: Hybrid Plasma Acceleration (Trojan Horse prehistory)

- Sequential combination:
Use double bunches generated via LWFA (e.g. by injection into multiple buckets) as driver/witness pairs in subsequent, dephasing-free PWFA stage

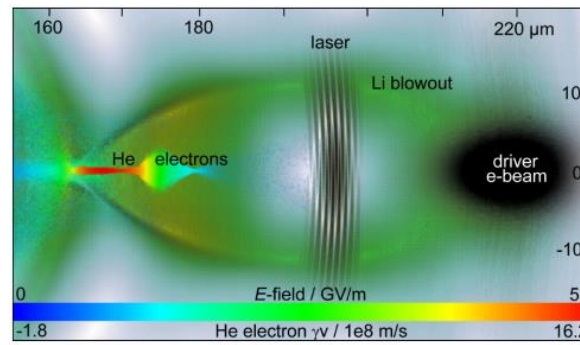


Hybrid energy doubling, PRL 104, 195002, 2010

- “Superimposed” interaction:
2008: Laser-driven bubble in a beam-driven blowout? (“Matryoshka acc..”)



- 2008/2009: much better mode would be to have the laser pulse at minimal intensity ($a_0 \ll 1$), so that released electrons are “still” and remain still inside the blowout \rightarrow “Trojan horse acc.”, originally considered for presentation at AAC 2010 in Kardamili, Greece (sic!)



Ultracold electron bunch generation aka Trojan Horse, PRL 108, 035001, 2012

5th Generation Light Sources...

...need a 4th Generation Electron Source

5th
4D, ultrahard,
compact?

4th
Free-Electron-
Laser

3rd
Undulator
radiation

2nd
Synchrotron
radiation

1st
Bremsstrahlung

4th
10's of GV/m fields in
plasmas & underdense
photocathode PWFA

3rd
10's of GV/m fields in
plasmas
(LWFA and PWFA)

2nd
10's of MV/m fields,
photocathode
(e.g. FLASH, LCLS, XFEL)

1st
10's of MV/m fields,
thermionic cathode
(e.g. SLAC)

Export Trojan

